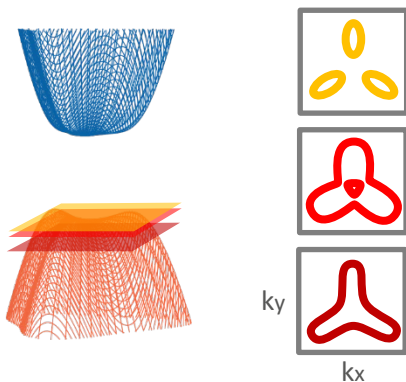


Correlated phases in the vicinity of tunable van Hove singularities in Bernal bilayer graphene



Anna M. Seiler

Nils Jacobsen, Martin Statz, Fabian R. Geisenhof, Felix Winterer, Isabell Weimer, Noelia Fernandez, Francesca Falorsi, Kenji Watanabe, Takashi Taniguchi, Tianyi Xu, Zhiyu Dong, Leonid S. Levitov, Fan Zhang, R. Thomas Weitz

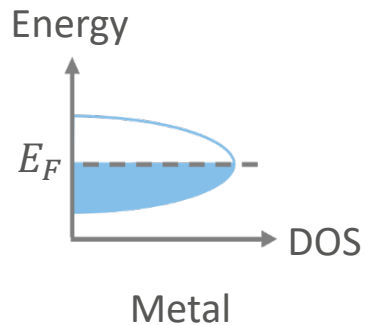
Geneva, 17.05.2024

Electronic correlations

- The behavior of an electron is dependent on the behavior of the others
- Electron-electron correlations can induce spontaneous symmetry breaking

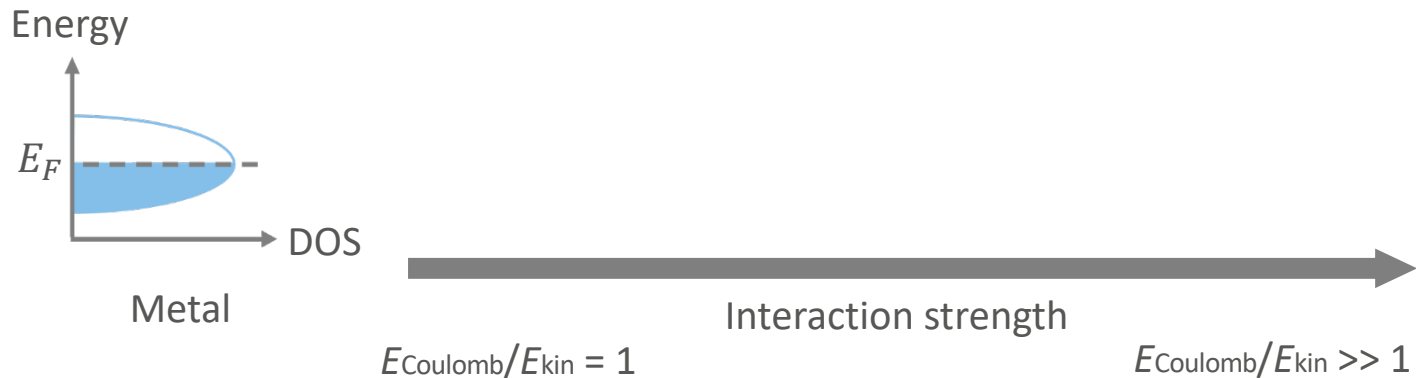
Electronic correlations

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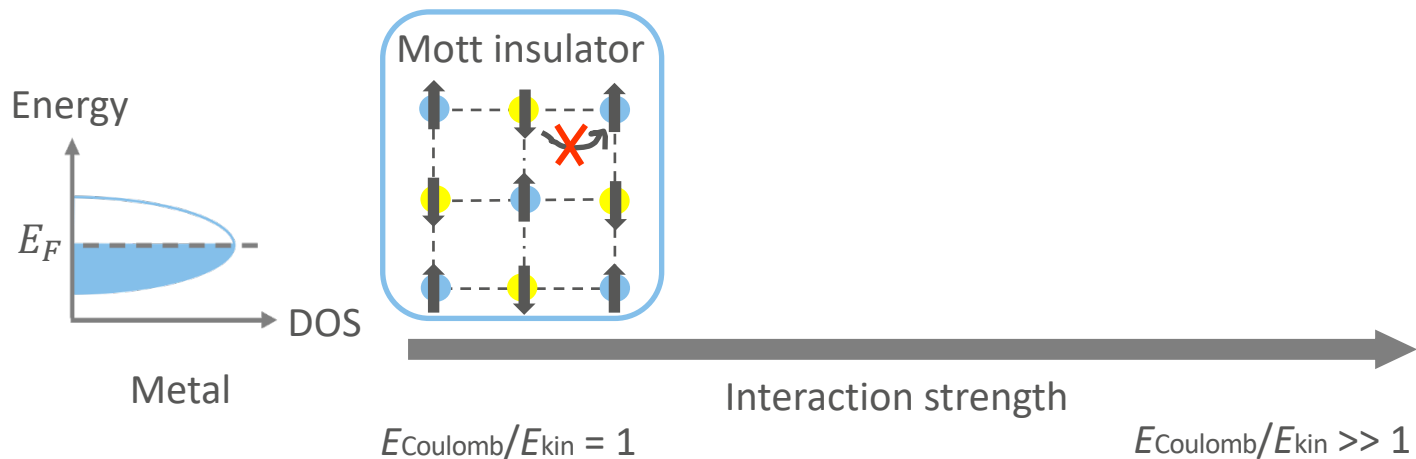
Electronic correlations

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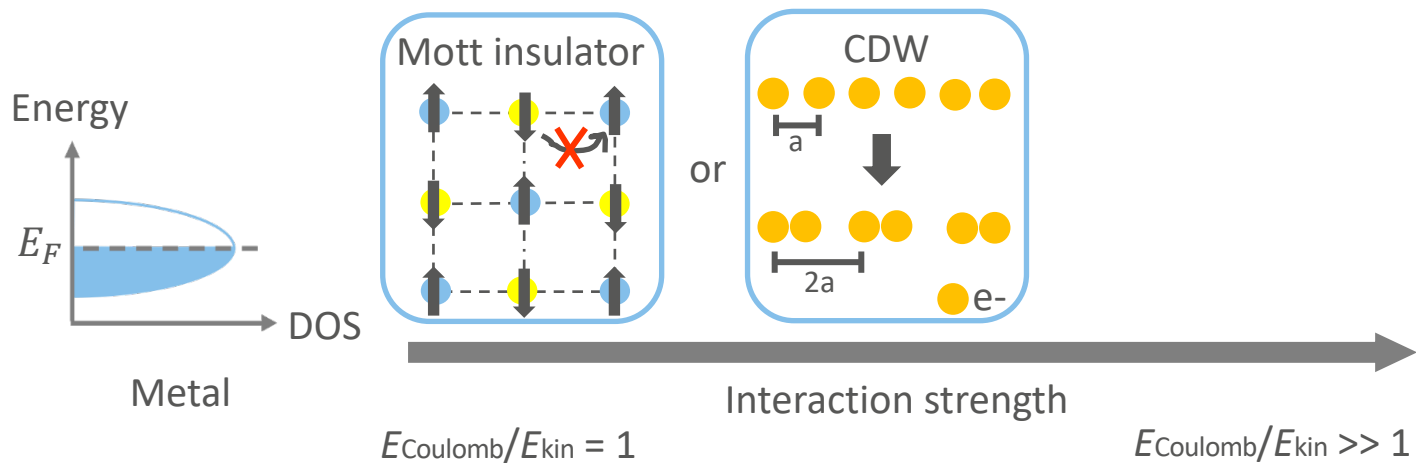
Electronic correlations

- The behavior of an electron is dependent on the behavior of the others
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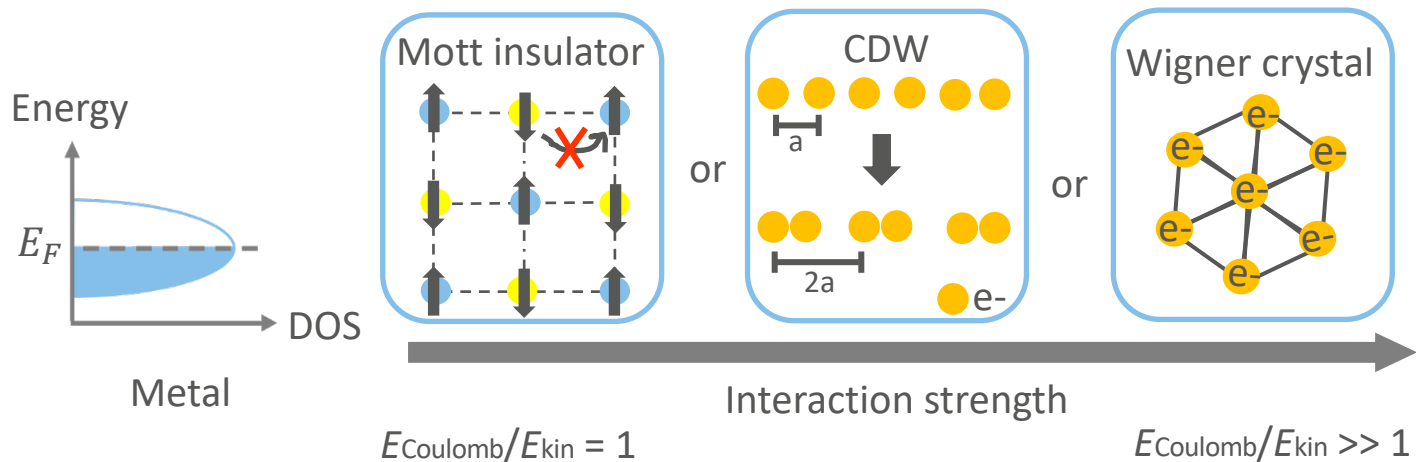
Electronic correlations

- The behavior of an electron is dependent on the behavior of the others
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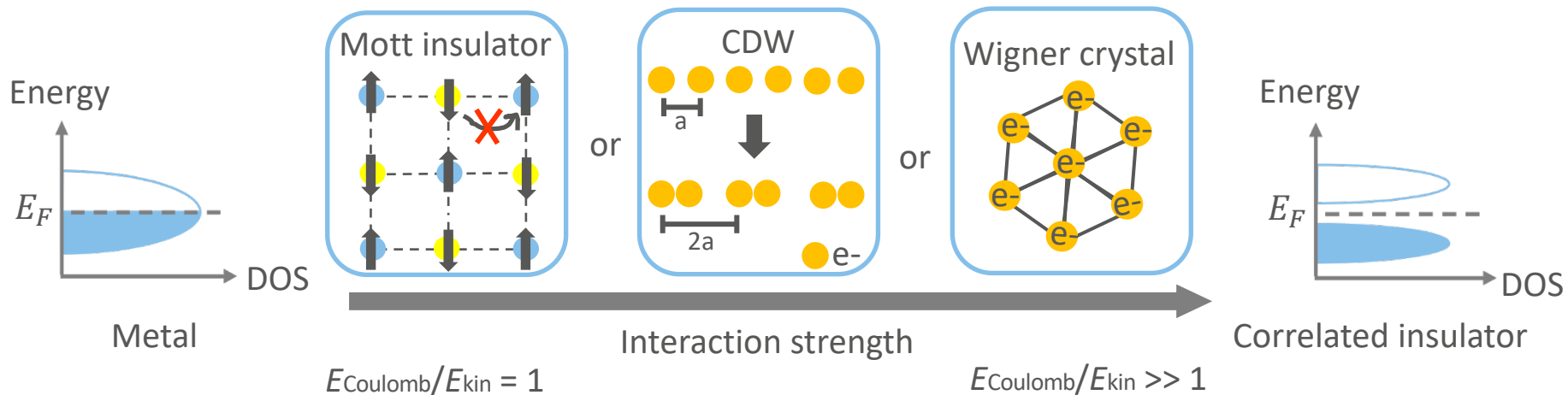
Electronic correlations

- The behavior of an electron is dependent on the behavior of the others
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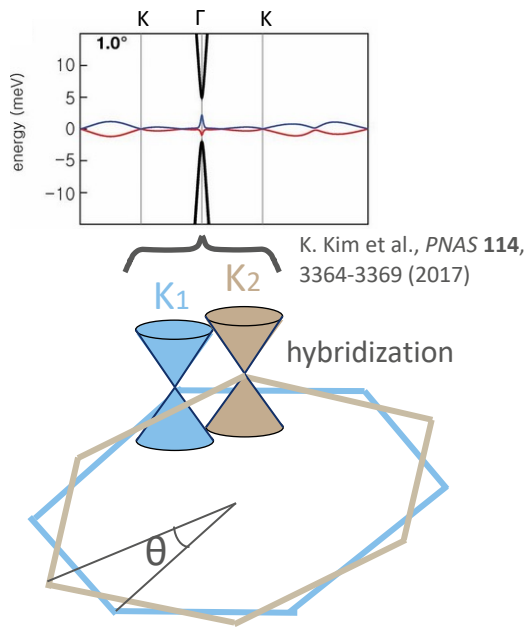


Electronic correlations

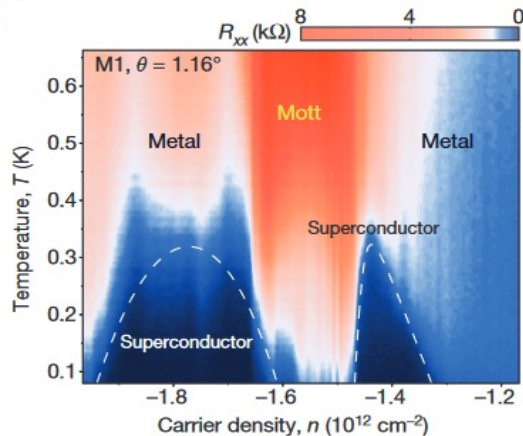
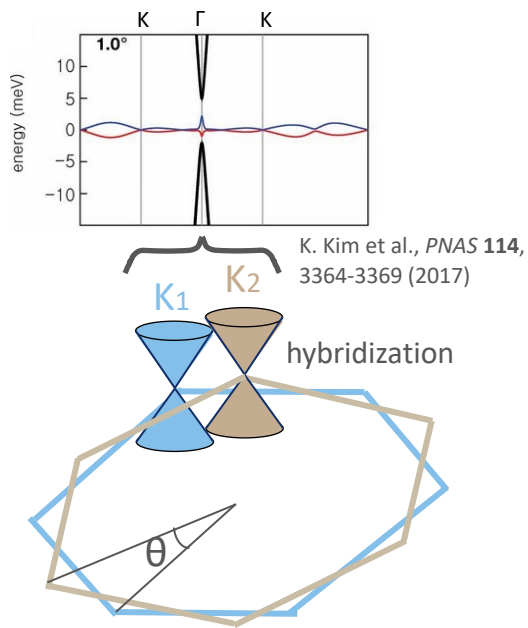
- The behavior of an electron is dependent on the behavior of the others
- Electron-electron correlations can induce spontaneous symmetry breaking



Magic-angle twisted bilayer graphene

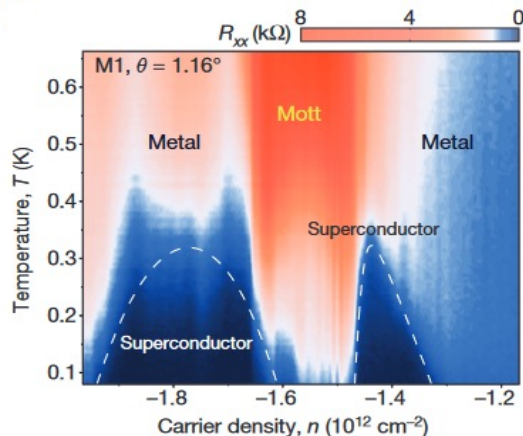
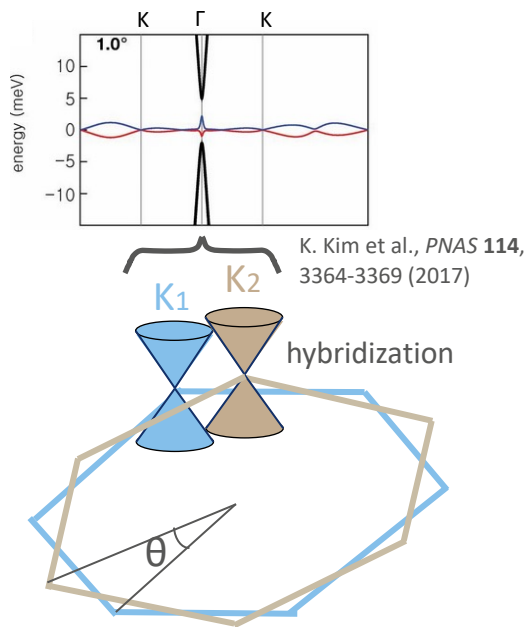


Magic-angle twisted bilayer graphene



Y. Cao et al., *Nature* **556**, 43-50 (2018)

Magic-angle twisted bilayer graphene

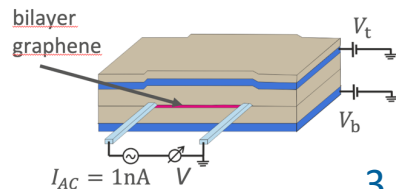


Y. Cao et al., *Nature* **556**, 43-50 (2018)

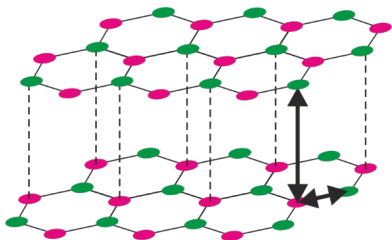
Are there similar correlated phases in natural bilayer graphene?

Outline

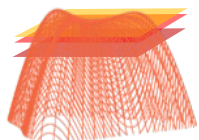
2. Transport measurements



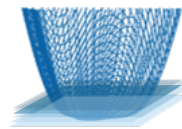
1. Bernal bilayer graphene



3. Correlated phases at hole-doping

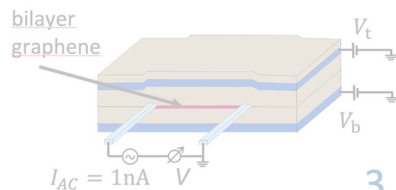


4. Correlated phases at electron-doping

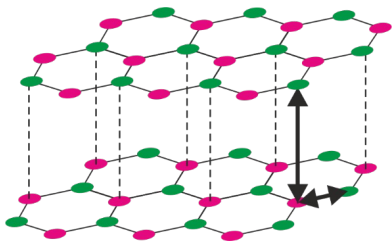


Outline

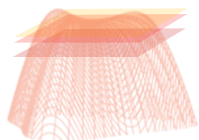
2. Transport measurements



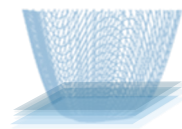
1. Bernal bilayer graphene



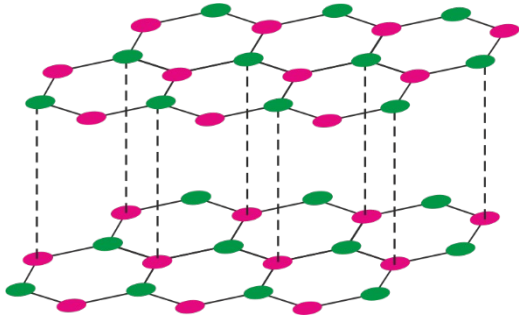
3. Correlated phases at hole-doping



4. Correlated phases at electron-doping

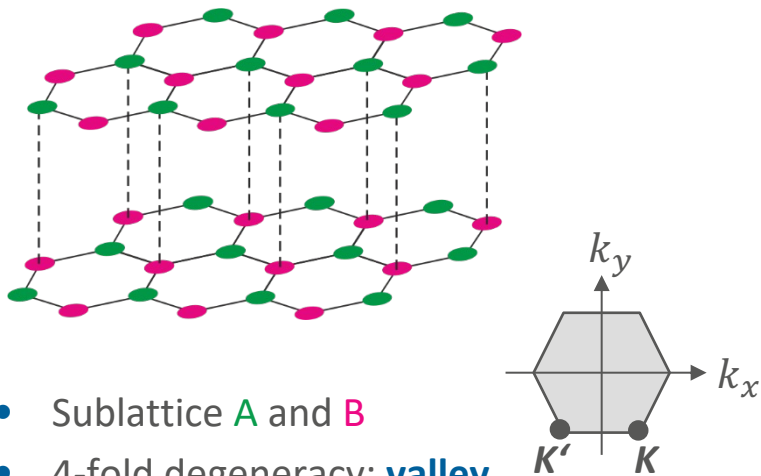


Bernal bilayer graphene



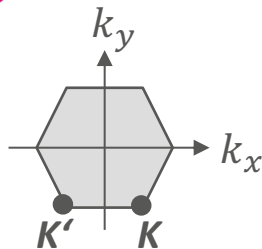
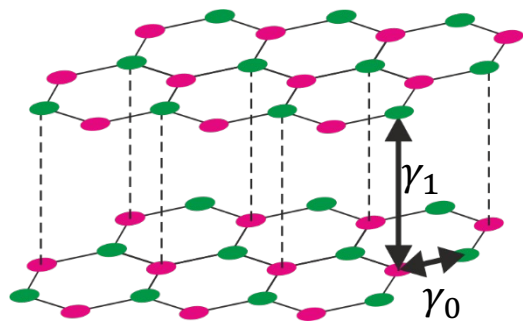
- Sublattice **A** and **B**

Bernal bilayer graphene

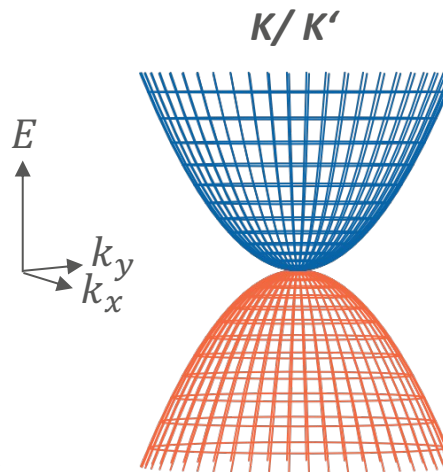


- Sublattice **A** and **B**
- 4-fold degeneracy: **valley** and **spin** degrees of freedom

Bernal bilayer graphene



- Sublattice **A** and **B**
- 4-fold degeneracy: **valley** and **spin** degrees of freedom



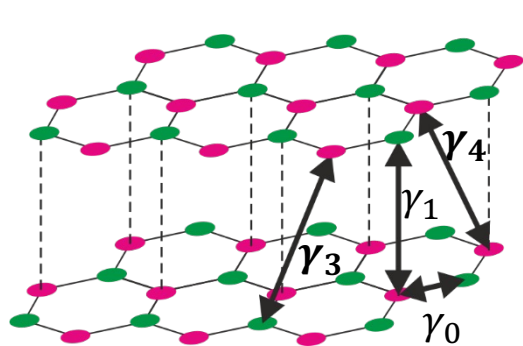
Band structure calculations done by Nils Jacobsen

Parabolic band structure!

consistent with

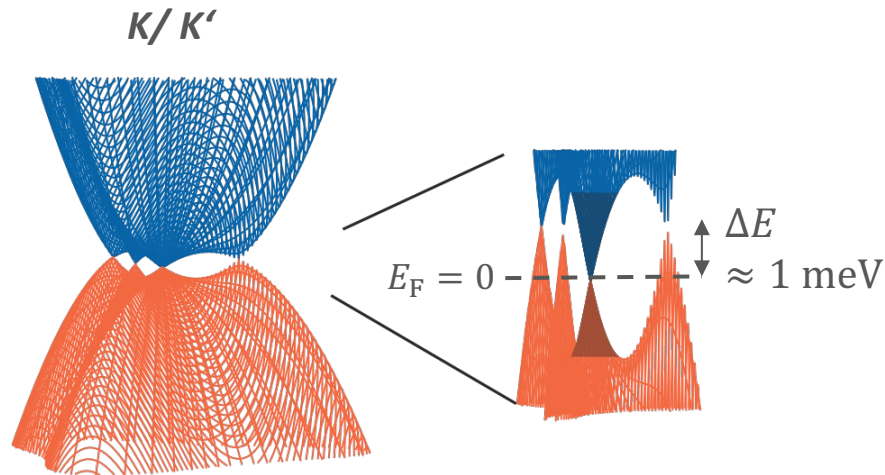
K. S. Novoselov et al. *Nature Physics* **2**, 177-180 (2006)
 R. T. Weitz et al. *Science* **330**, 812-816 (2010)
 J. I. A. Li et al. *Science* **358**, 648-652 (2017)
 F. R. Geisenhof et al. *Nature* **598**, 53-58 (2021)
 and many others...

Bernal bilayer graphene



γ_3 → trigonal warping
 γ_4 → electron-hole asymmetry

E
 k_y
 k_x

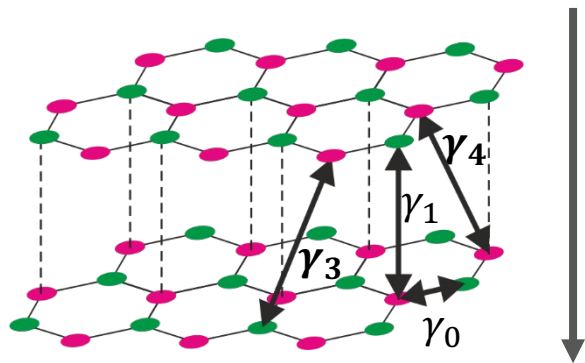


Band structure calculations done by Nils Jacobsen

- Sublattice **A** and **B**
- 4-fold degeneracy: **valley** and **spin** degrees of freedom

see also: E. McCann and V. I. Fal'ko. *PRL* **96**, 086805 (2006) and others

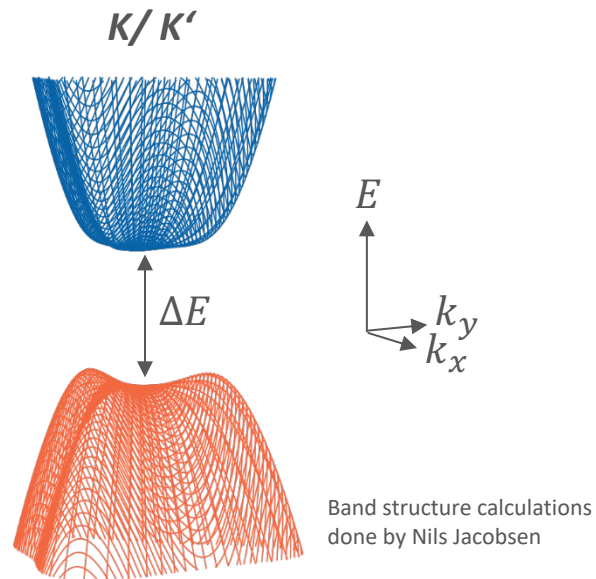
Bernal bilayer graphene



Electric displacement
field D

breaks inversion
symmetry

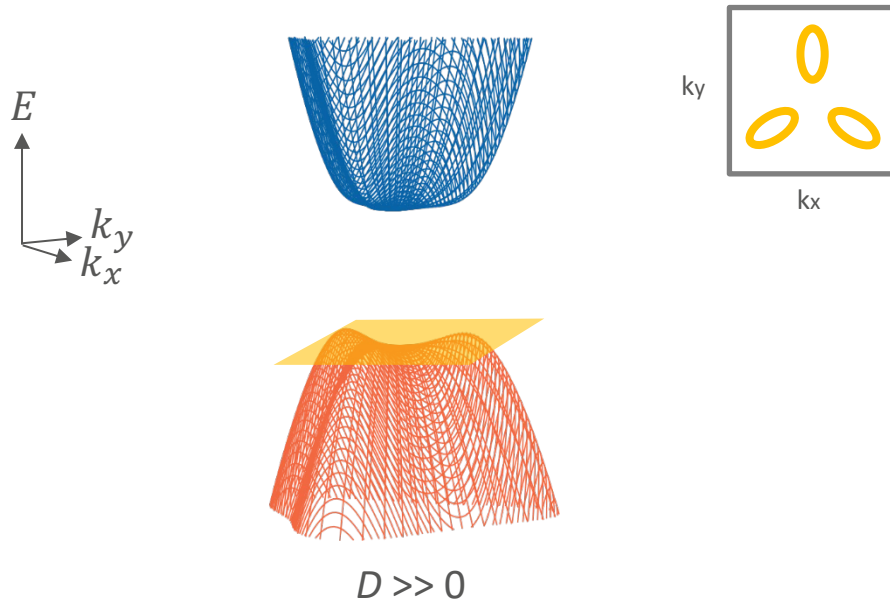
- Sublattice **A** and **B**
- 4-fold degeneracy: **valley**
and **spin** degrees of freedom



see also:

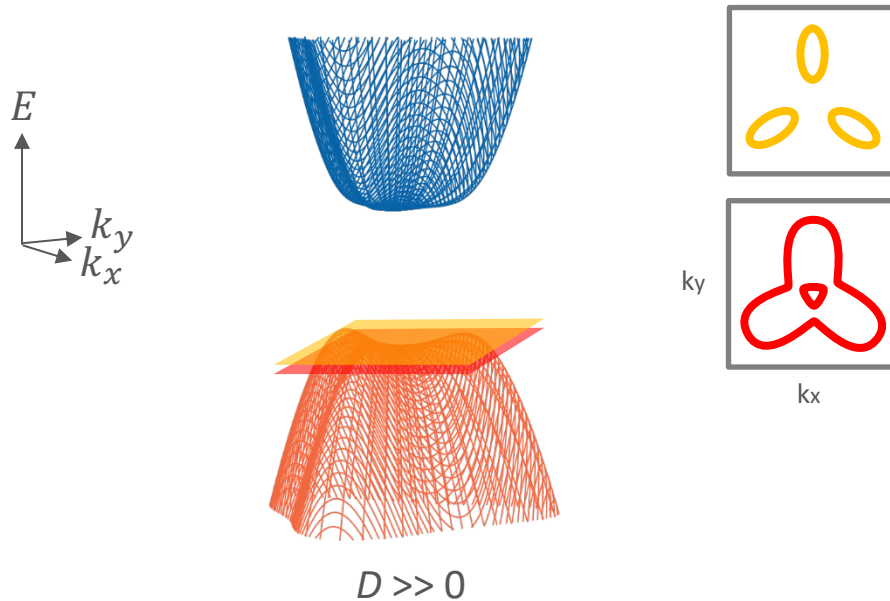
E. McCann and V. I. Fal'ko. *PRL* **96**, 086805 (2006) and others
A. Varlet et al. *PRL* **113**, 116602 (2014)

Van Hove singularities in bilayer graphene at $D \gg 0$



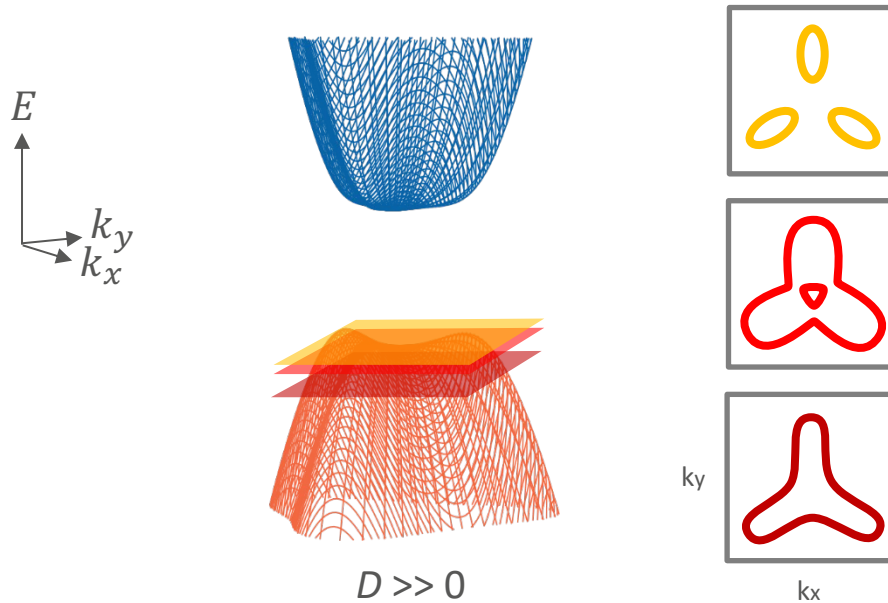
Band structure calculations done by Nils Jacobsen

Van Hove singularities in bilayer graphene at $D \gg 0$



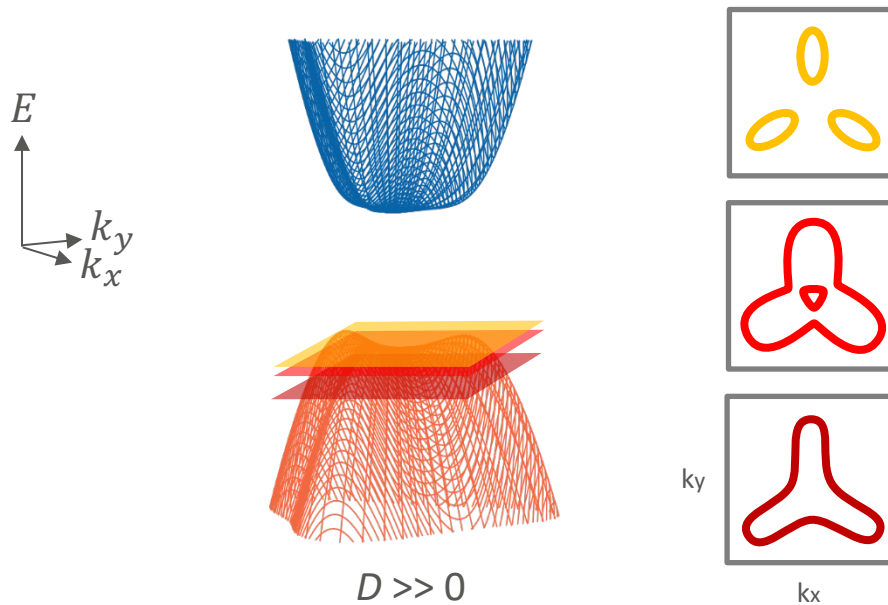
Band structure calculations done by Nils Jacobsen

Van Hove singularities in bilayer graphene at $D \gg 0$



Band structure calculations done by Nils Jacobsen

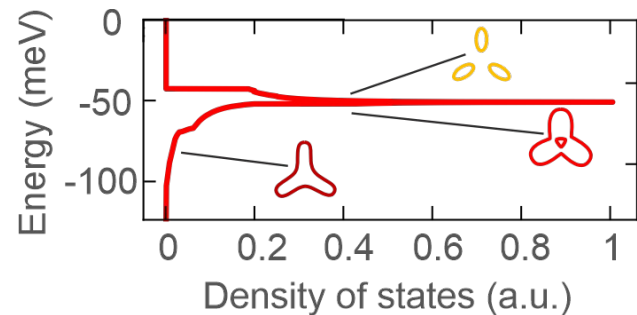
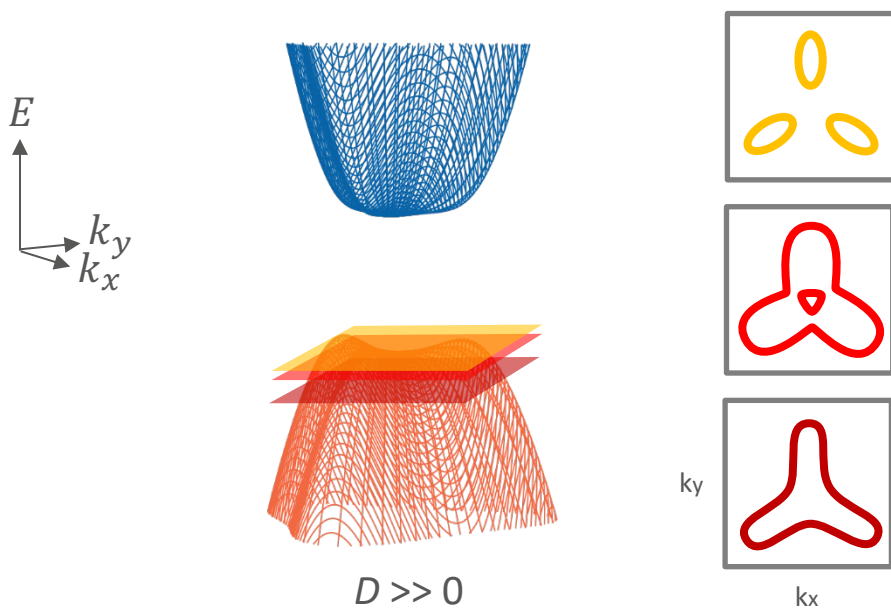
Van Hove singularities in bilayer graphene at $D \gg 0$



- Lifshitz transitions

Band structure calculations done by Nils Jacobsen

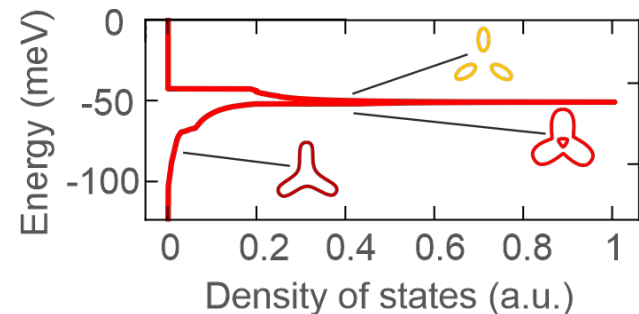
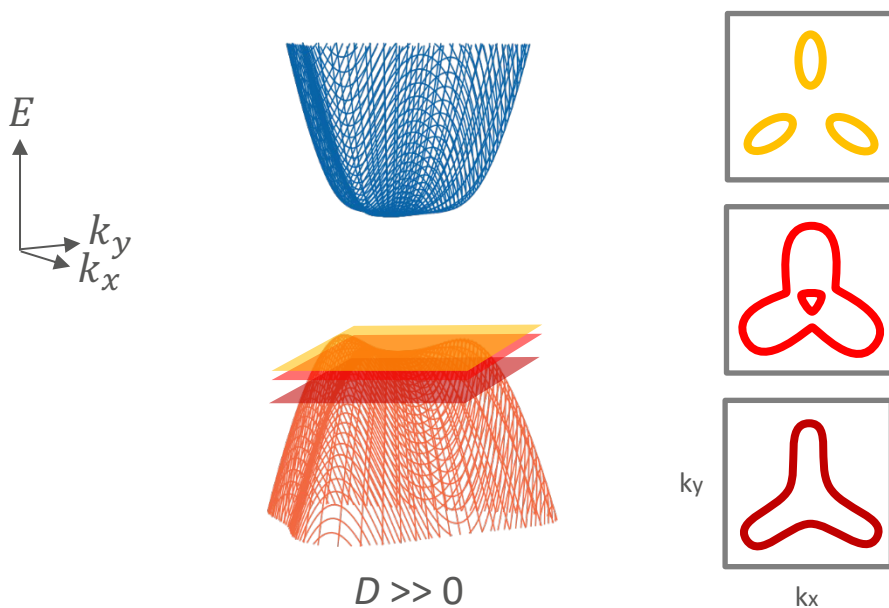
Van Hove singularities in bilayer graphene at $D \gg 0$



- Lifshitz transitions
- Van Hove singularities

Band structure and DOS calculations done by Nils Jacobsen

Van Hove singularities in bilayer graphene at $D \gg 0$

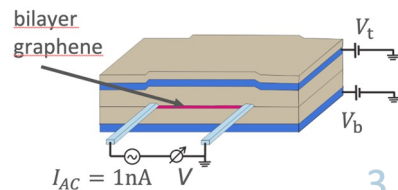


- Lifshitz transitions
- Van Hove singularities
- Interaction effects!

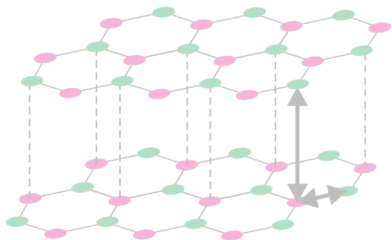
Band structure and DOS calculations done by Nils Jacobsen

Outline

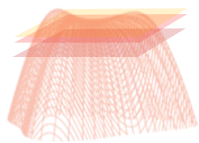
2. Transport measurements



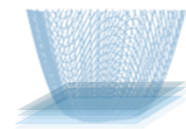
1. Bernal bilayer graphene



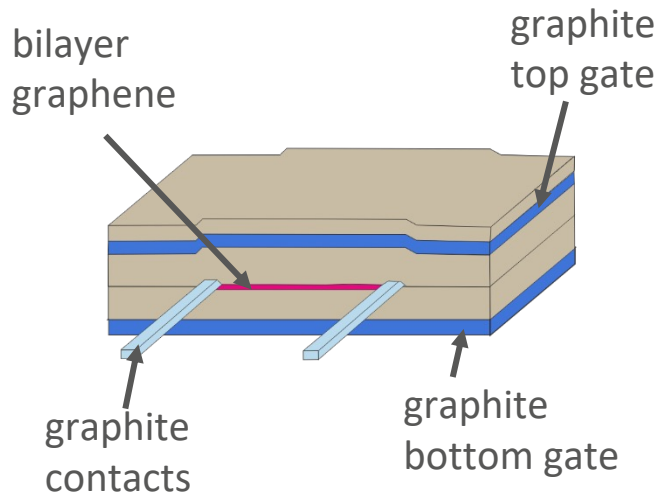
3. Correlated phases at hole-doping



4. Correlated phases at electron-doping

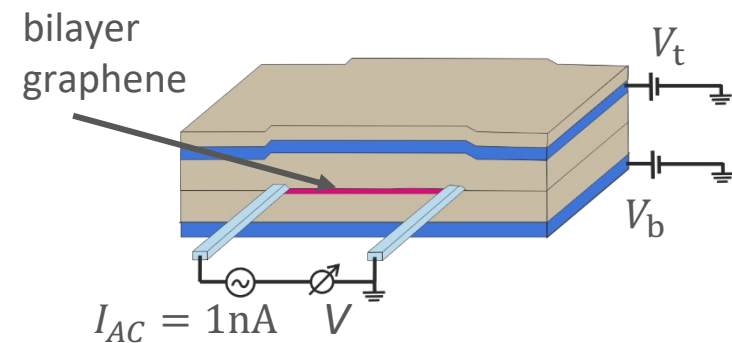


Fabrication of bilayer graphene heterostructures



hexagonal boron nitride (hBN)

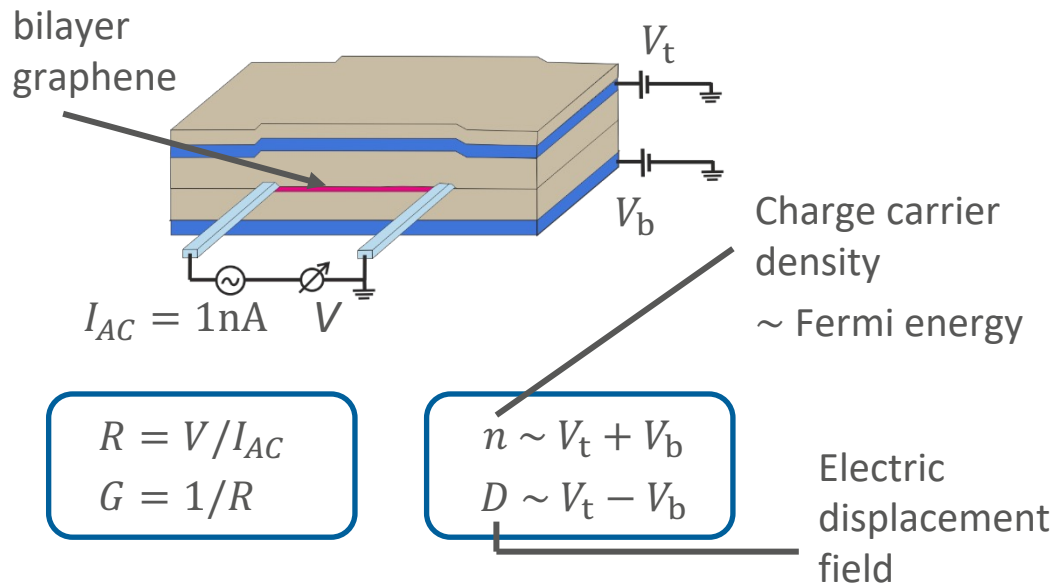
Electrical transport measurements



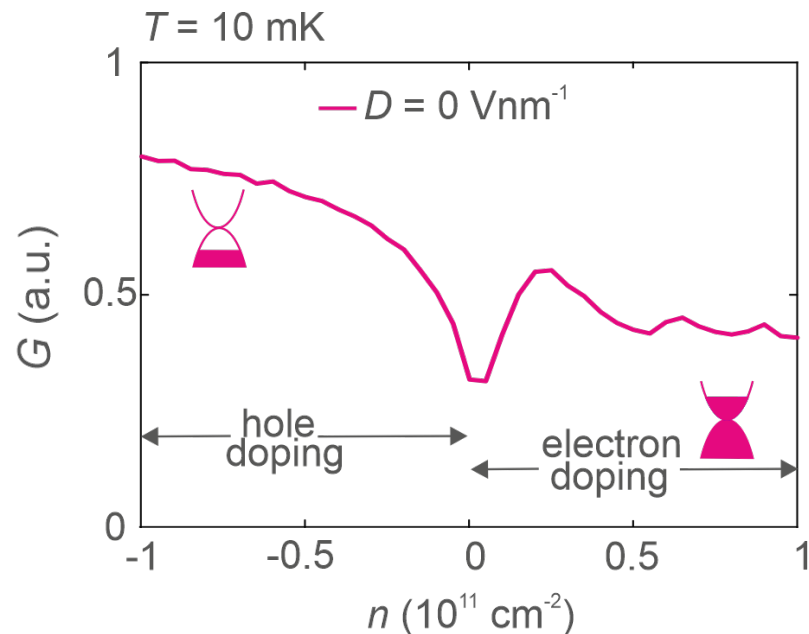
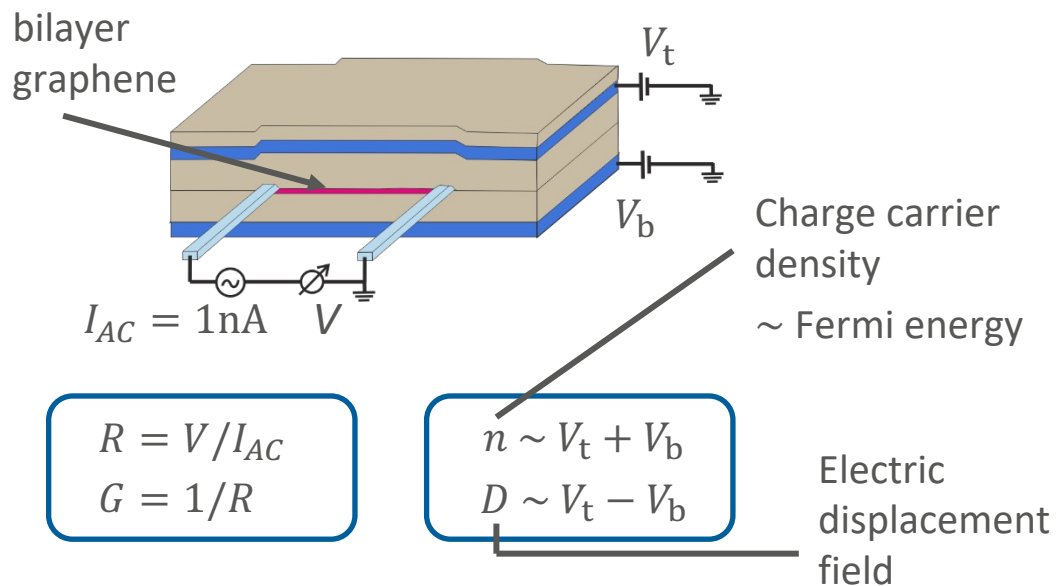
$$R = V/I_{AC}$$

$$G = 1/R$$

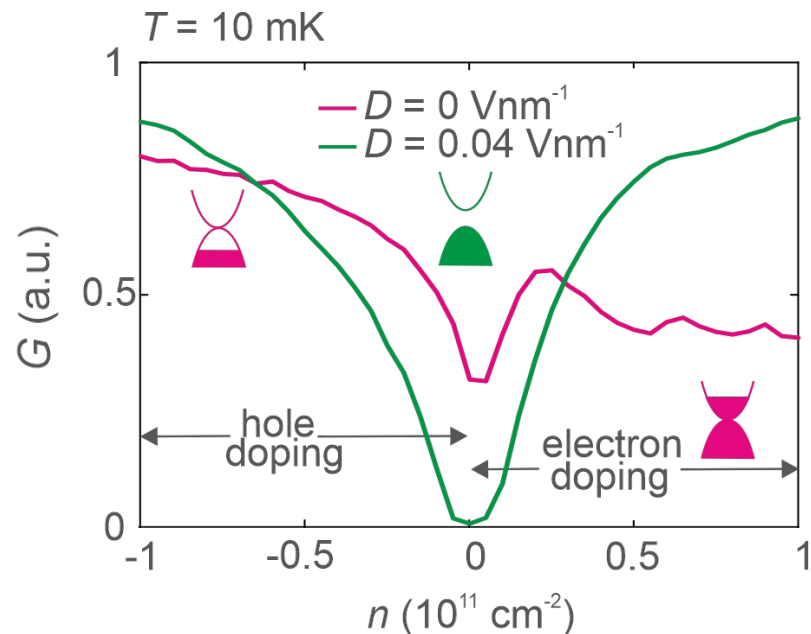
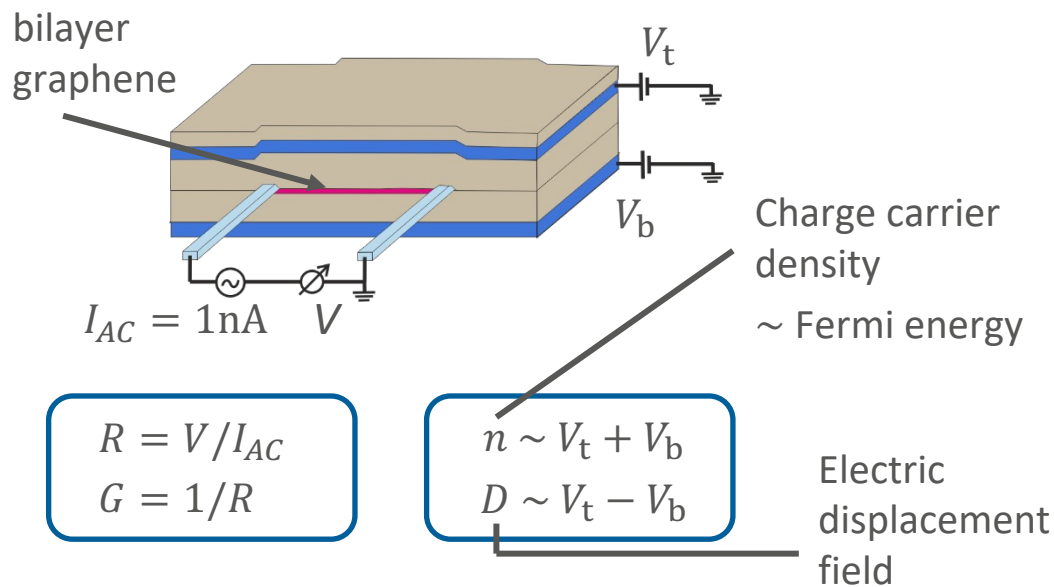
Electrical transport measurements



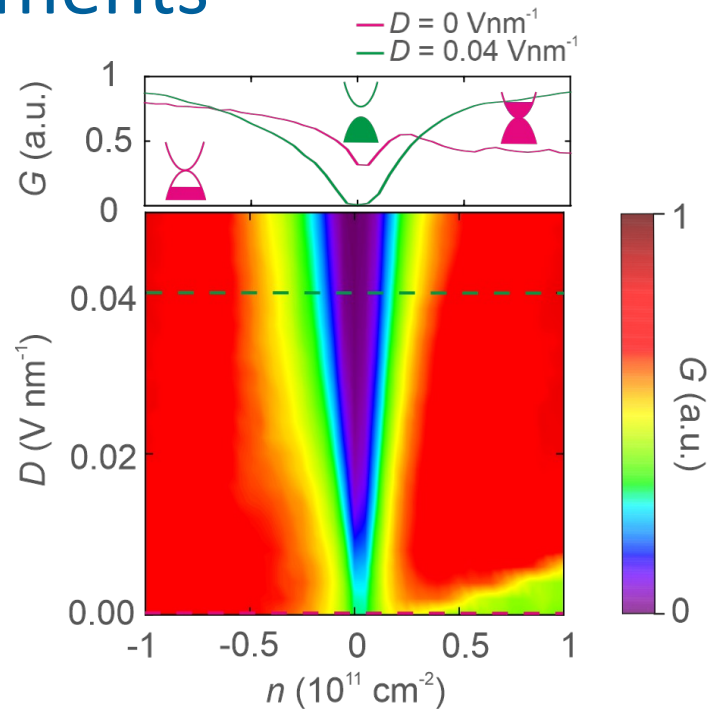
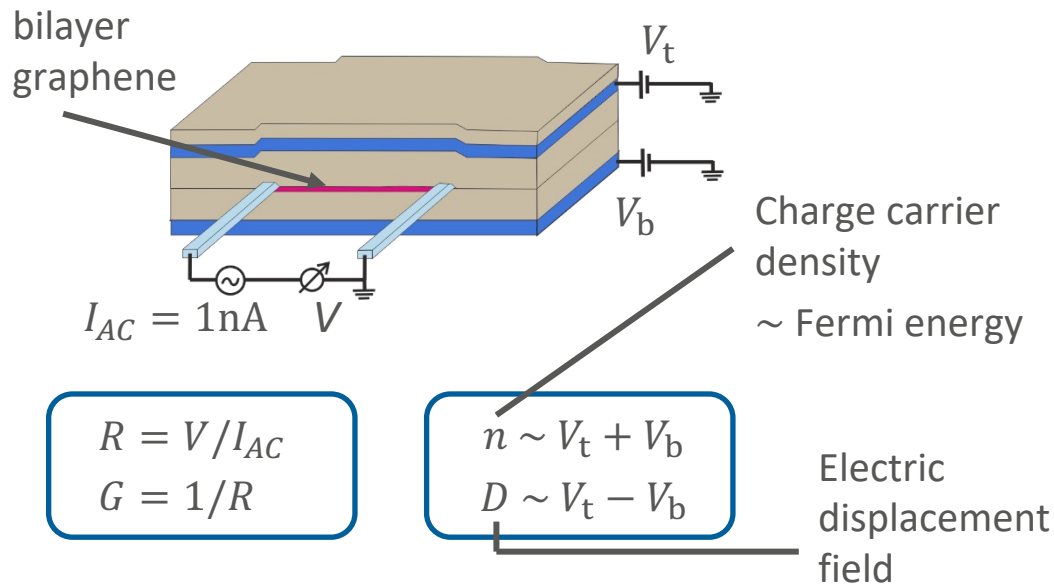
Electrical transport measurements



Electrical transport measurements

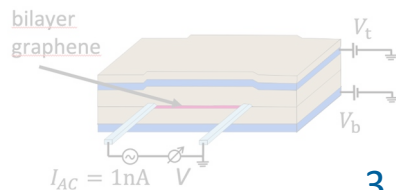


Electrical transport measurements

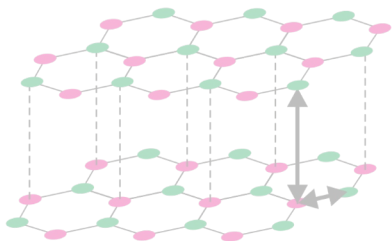


Outline

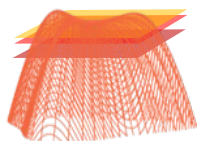
2. Transport measurements



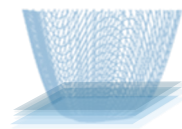
1. Bernal bilayer graphene

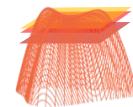


3. Correlated phases at hole-doping

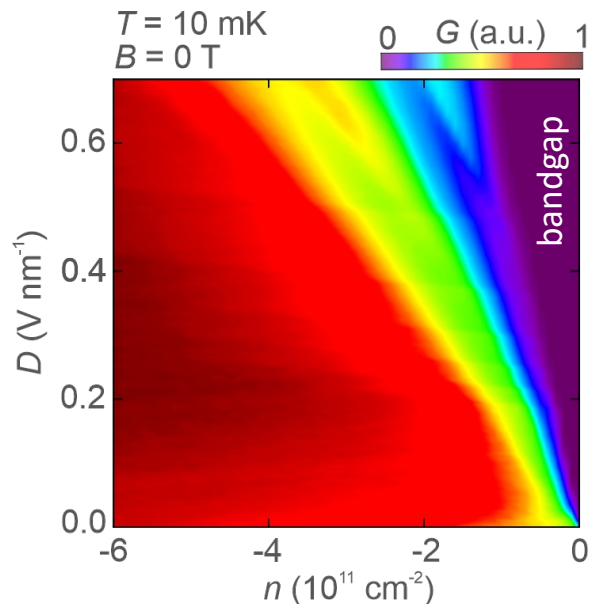


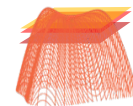
4. Correlated phases at electron-doping



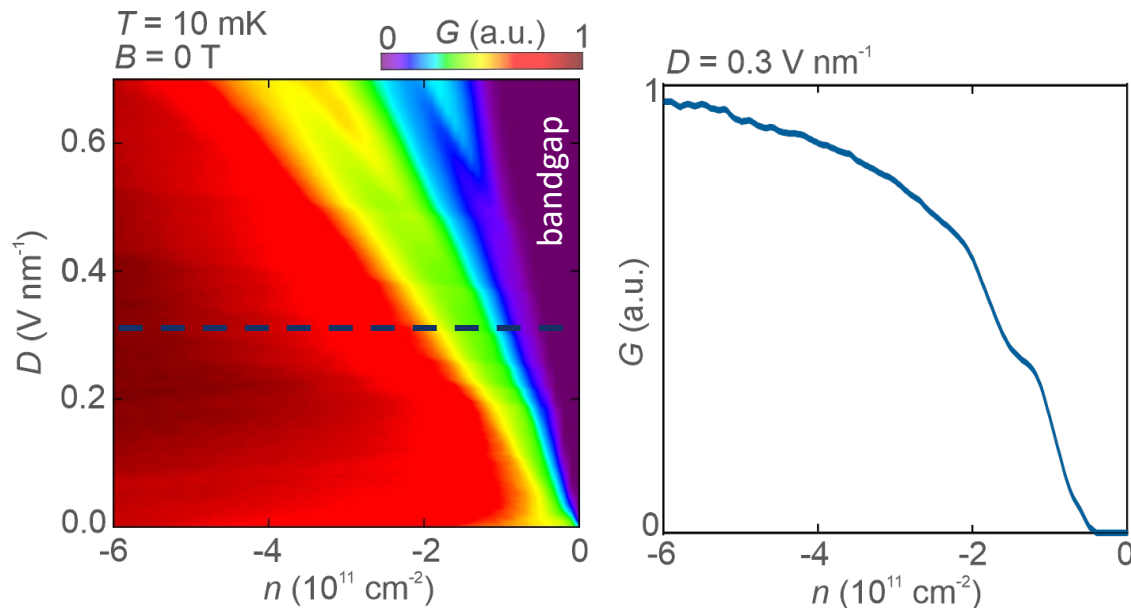


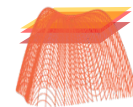
Correlated phases in hole-doped bilayer graphene



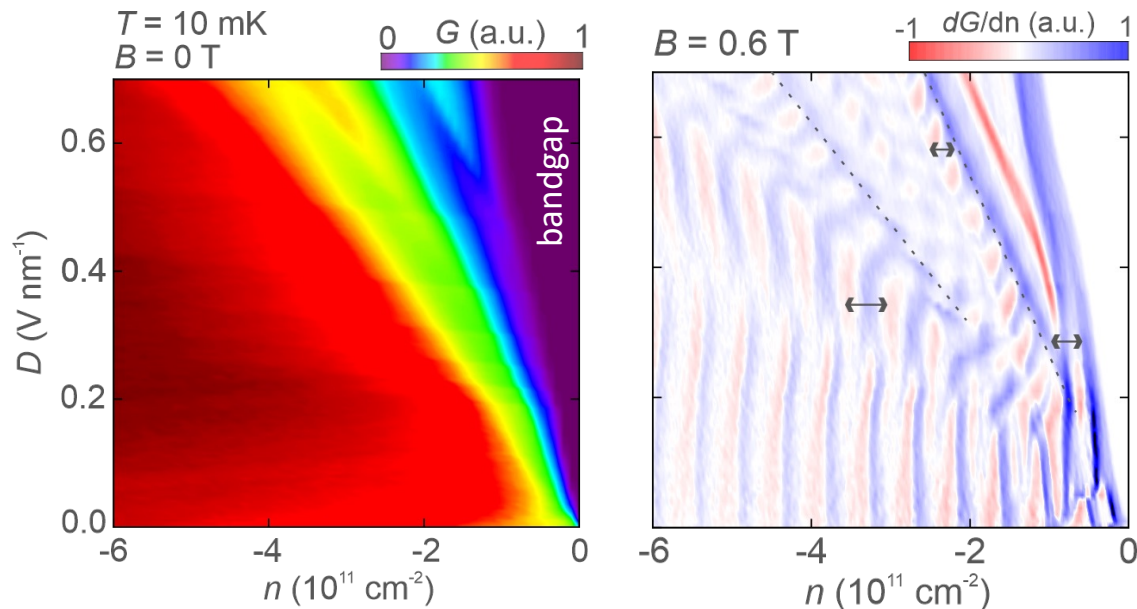


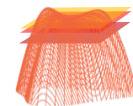
Correlated phases in hole-doped bilayer graphene



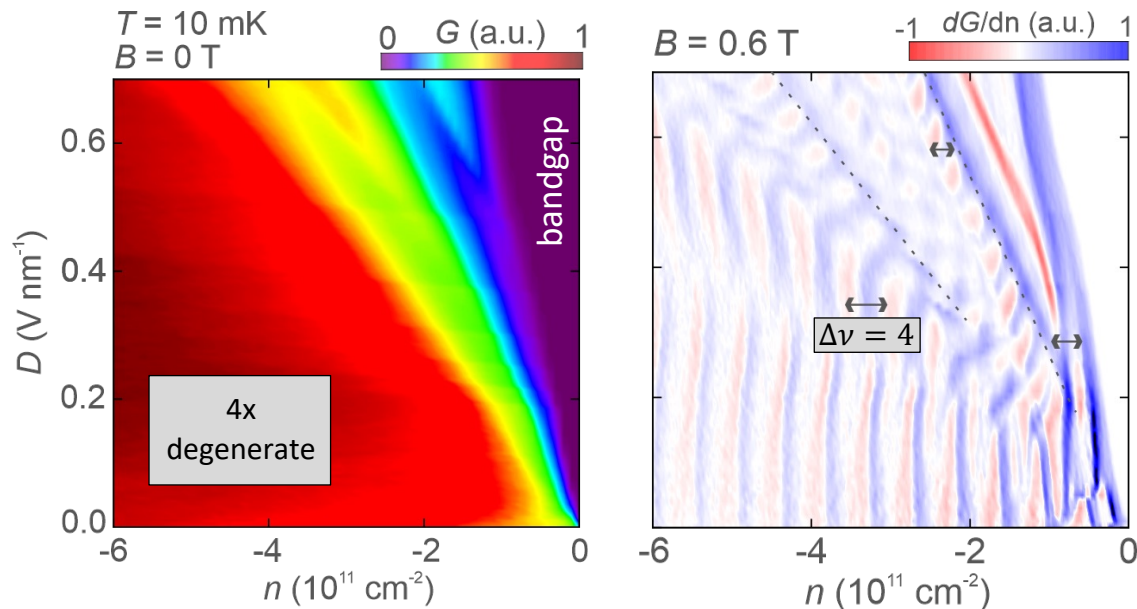


Correlated phases in hole-doped bilayer graphene

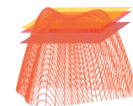




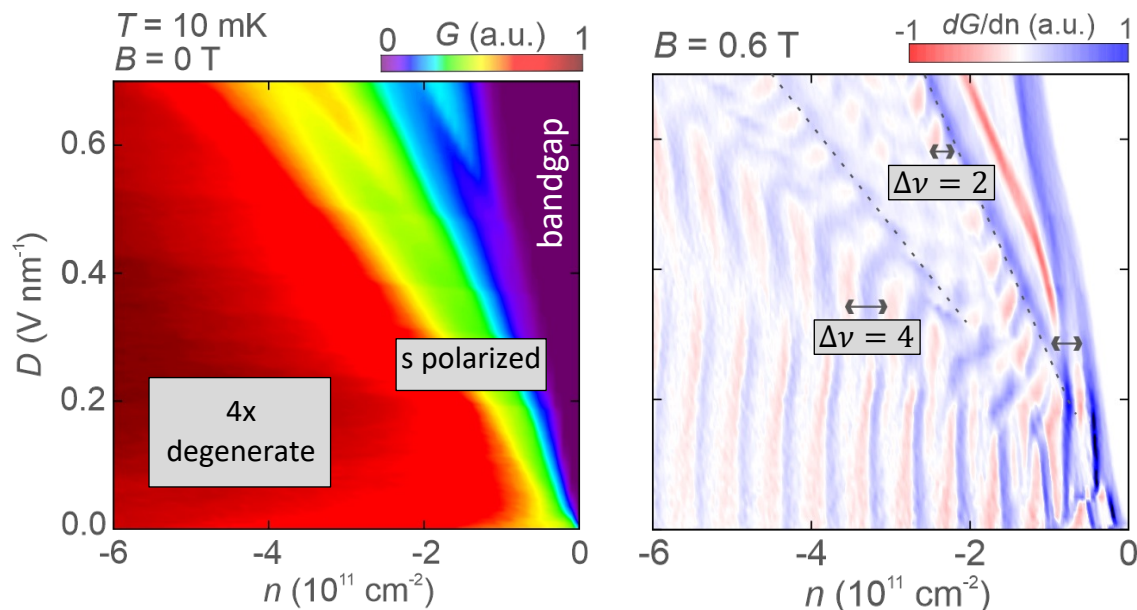
Correlated phases in hole-doped bilayer graphene



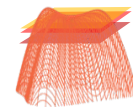
- 4x degenerate/ non-polarized phase \rightarrow full metal



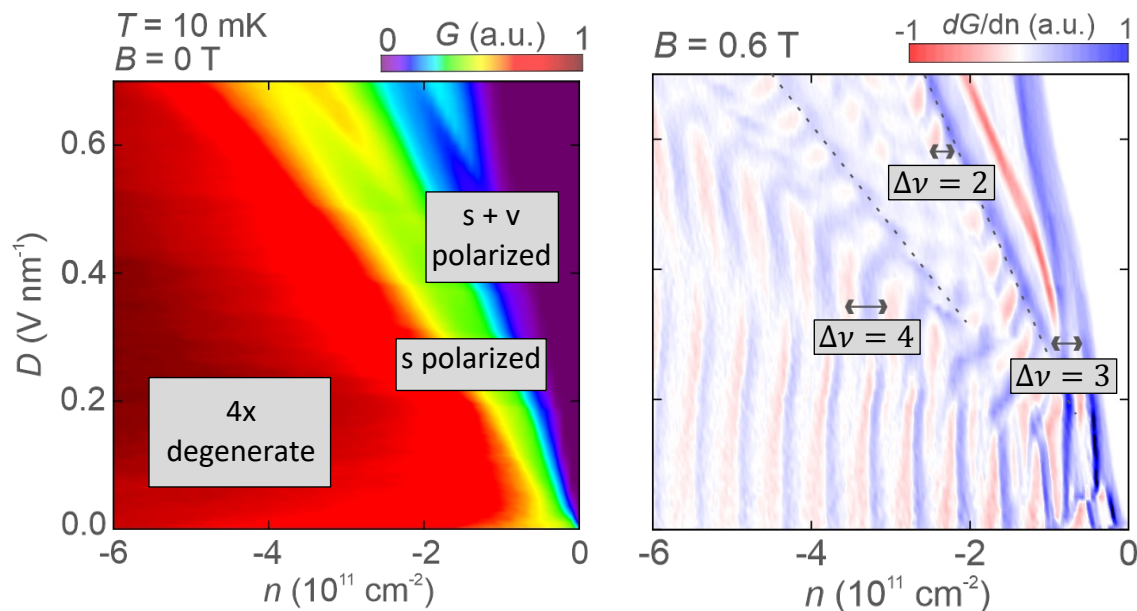
Correlated phases in hole-doped bilayer graphene



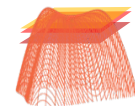
- 4x degenerate/ non-polarized phase \rightarrow full metal
- Spin (s) polarized phase \rightarrow Stoner half metal



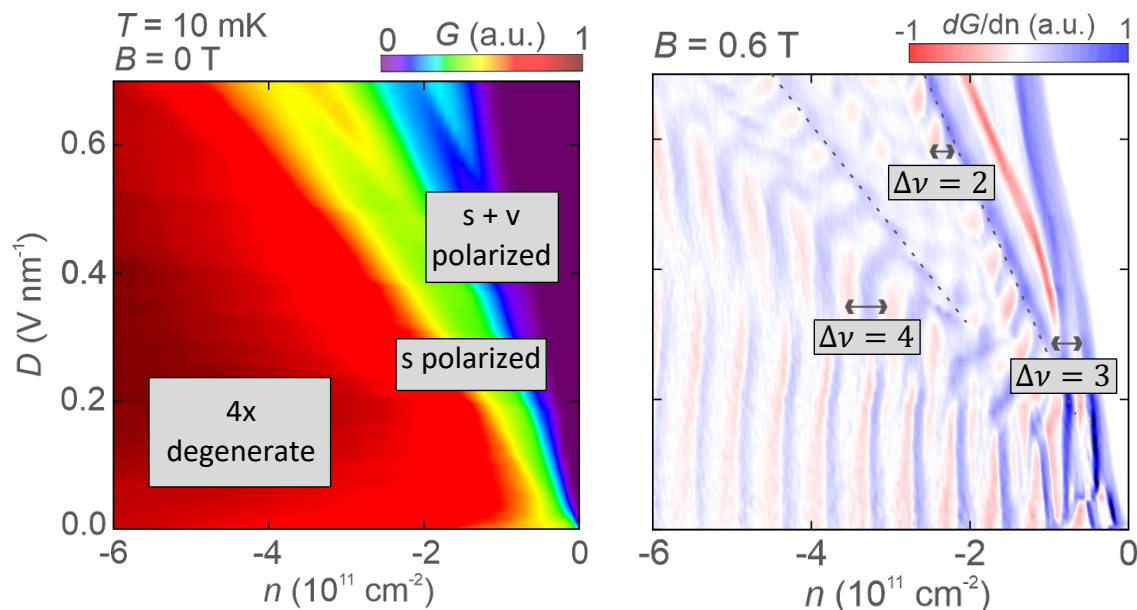
Correlated phases in hole-doped bilayer graphene



- 4x degenerate/ non-polarized phase -> full metal
- Spin (s) polarized phase -> Stoner half metal
- Spin (s) and valley (v) polarized phase -> Stoner quarter metal



Correlated phases in hole-doped bilayer graphene

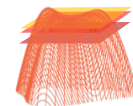


- 4x degenerate/ non-polarized phase -> full metal
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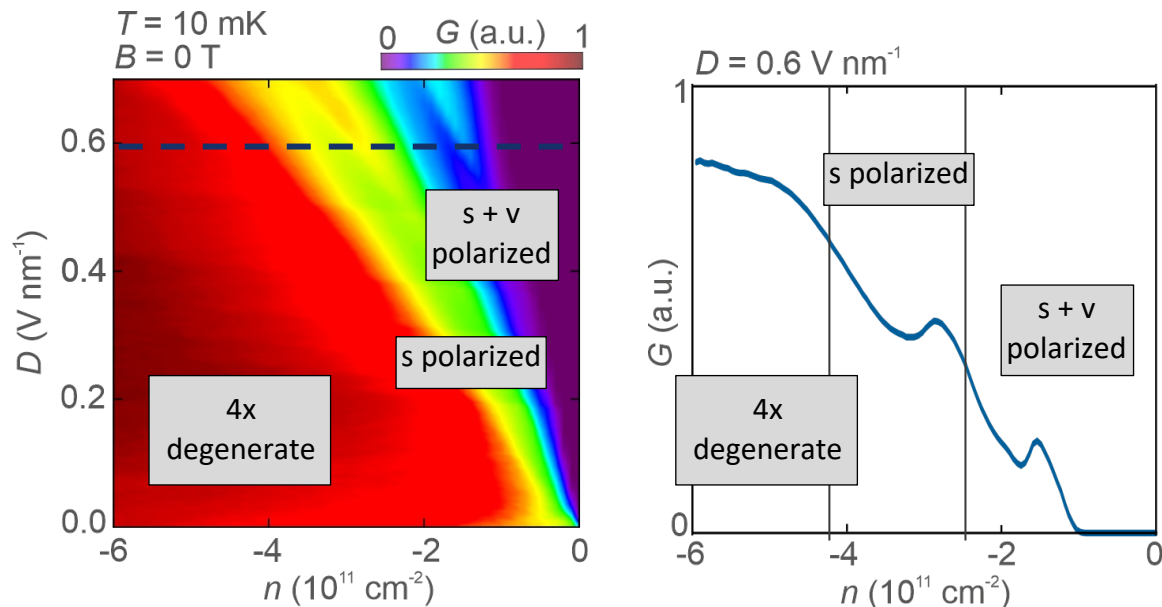
Consistent with

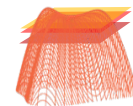
H. Zhou et al., *Science* **375**, 6582 (2022)

S. C. de la Barrera et al., *Nature Physics* **18**, 771-775 (2022)

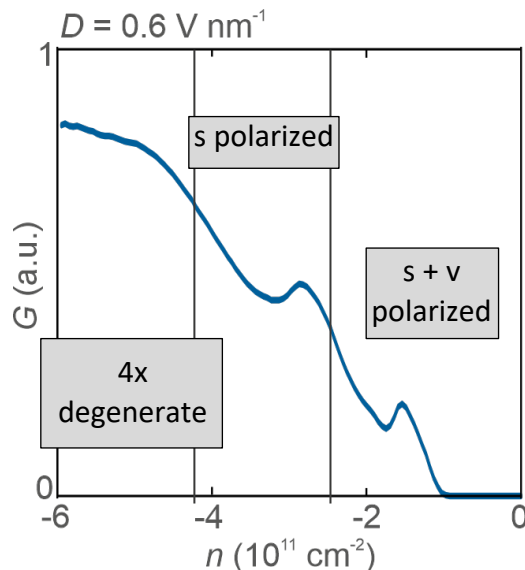
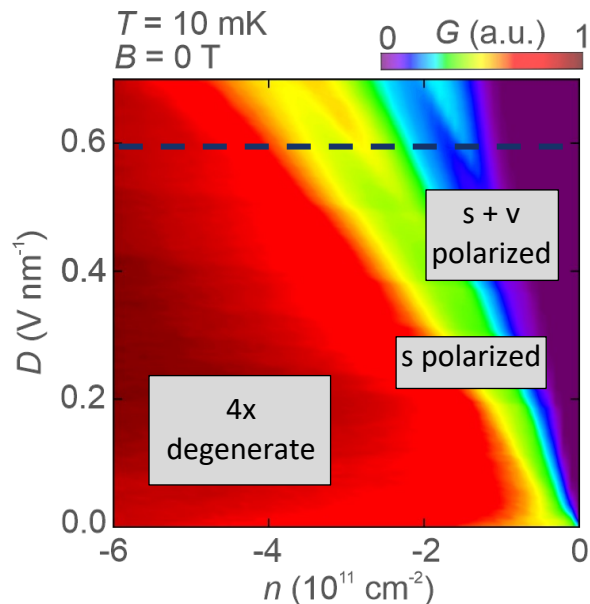


Correlated phases beyond Stoner physics

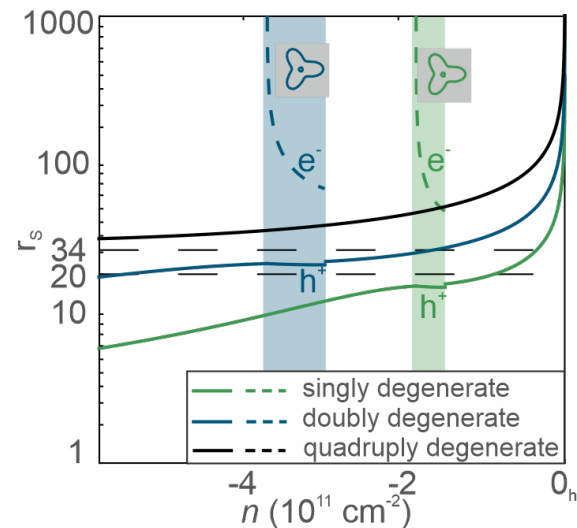


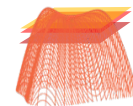


Correlated phases beyond Stoner physics

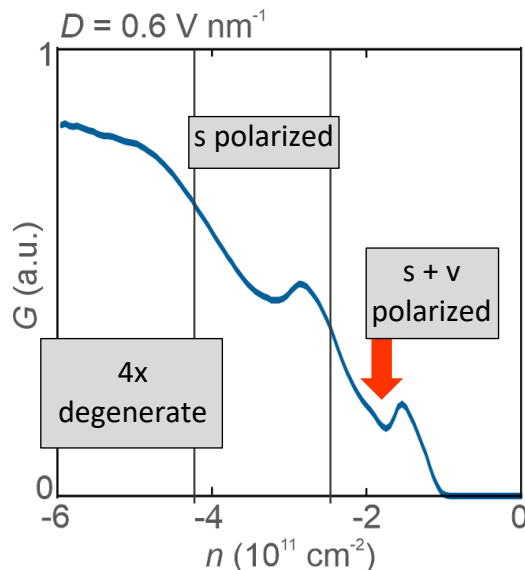
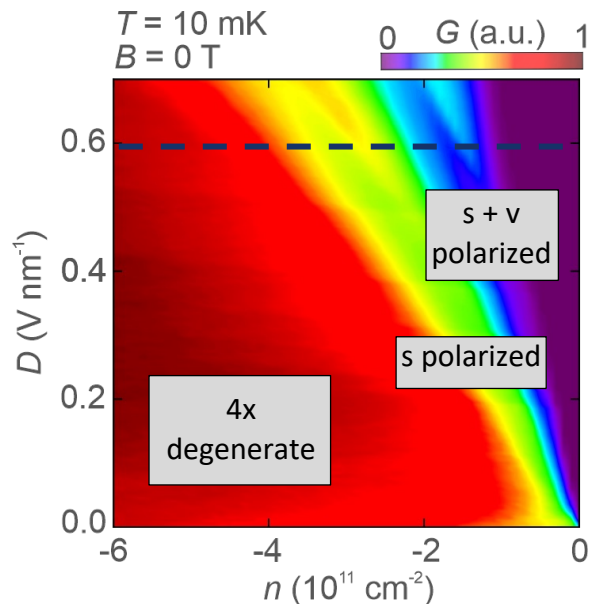


Theory:

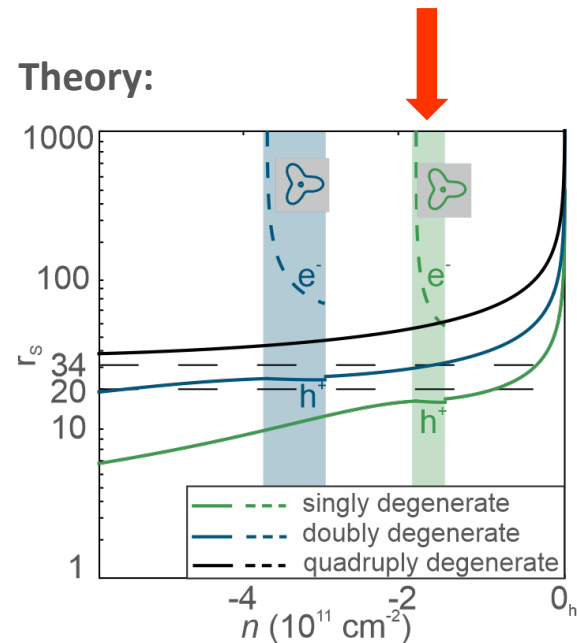


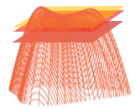


Correlated phases beyond Stoner physics

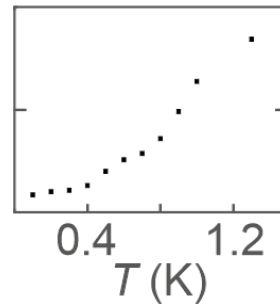
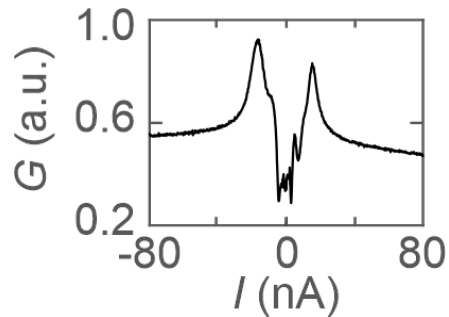


Theory:

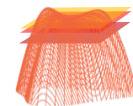




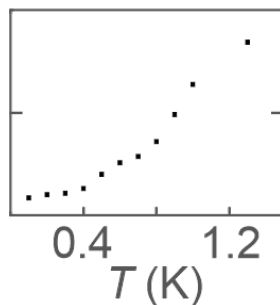
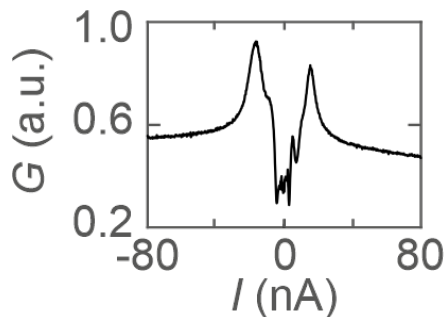
Insulating phase at $B = 0$ T



- Non-linear bias-current dependence
- Insulating temperature dependence

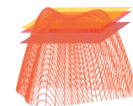


Insulating phase at $B = 0$ T

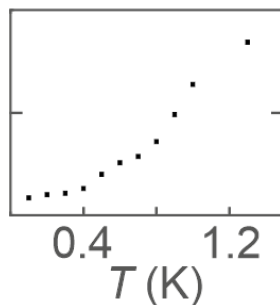
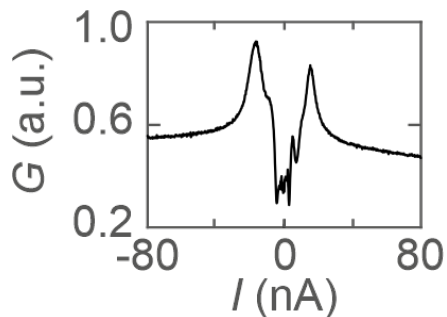


- Non-linear bias-current dependence
- Insulating temperature dependence

➔ Consistent with Wigner crystal



Insulating phase at $B = 0$ T

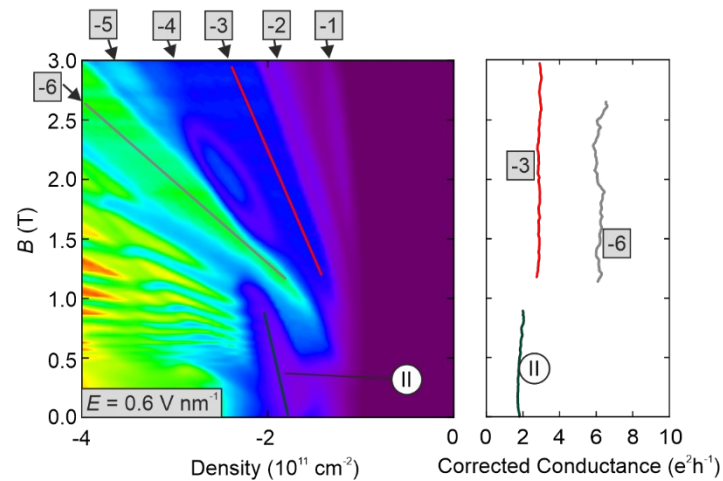


- Non-linear bias-current dependence
- Insulating temperature dependence

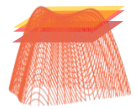
➔ Consistent with Wigner crystal

$D = 0.6$ V/nm

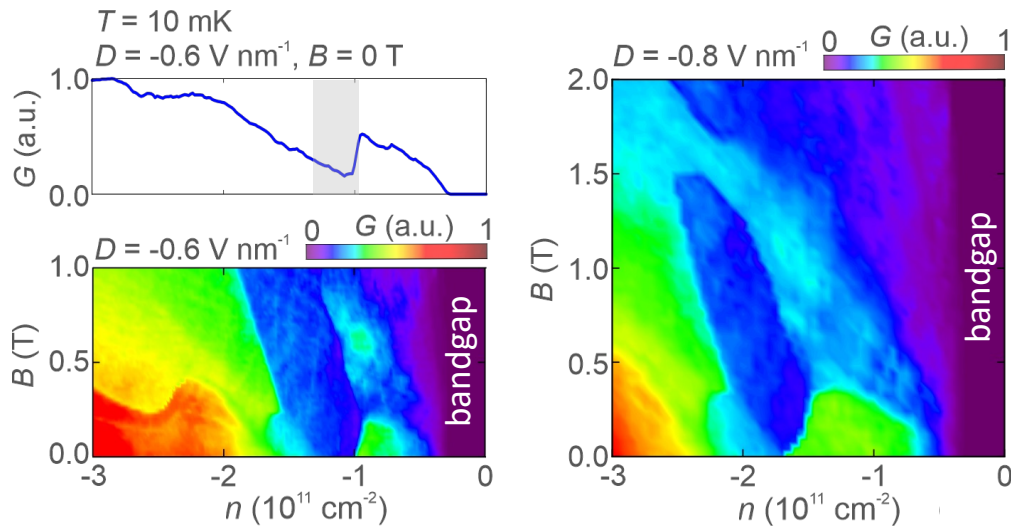
Corrected Conductance ($e^2 h^{-1}$)

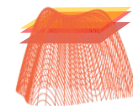


➔ $G \approx 2e^2/h$

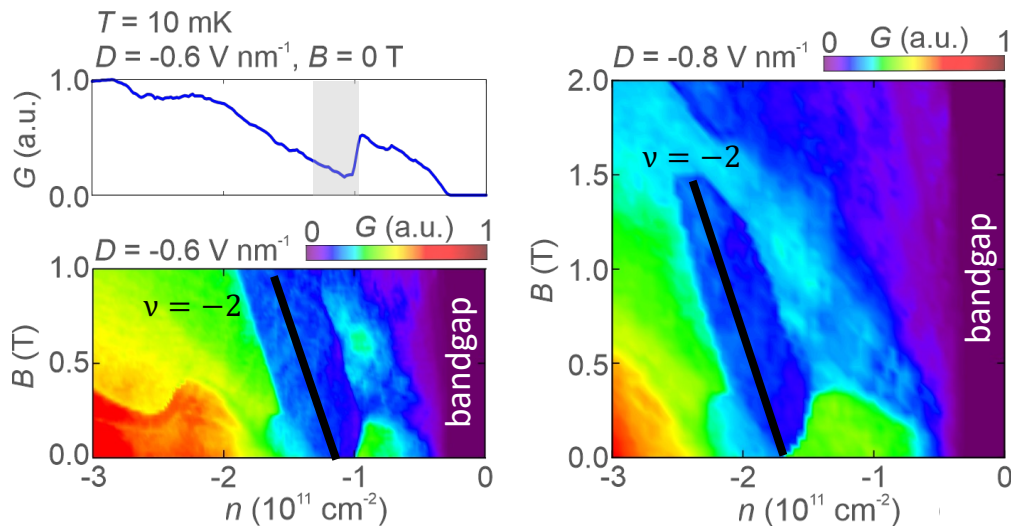


Applying an out-of-plane magnetic field

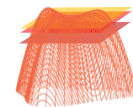




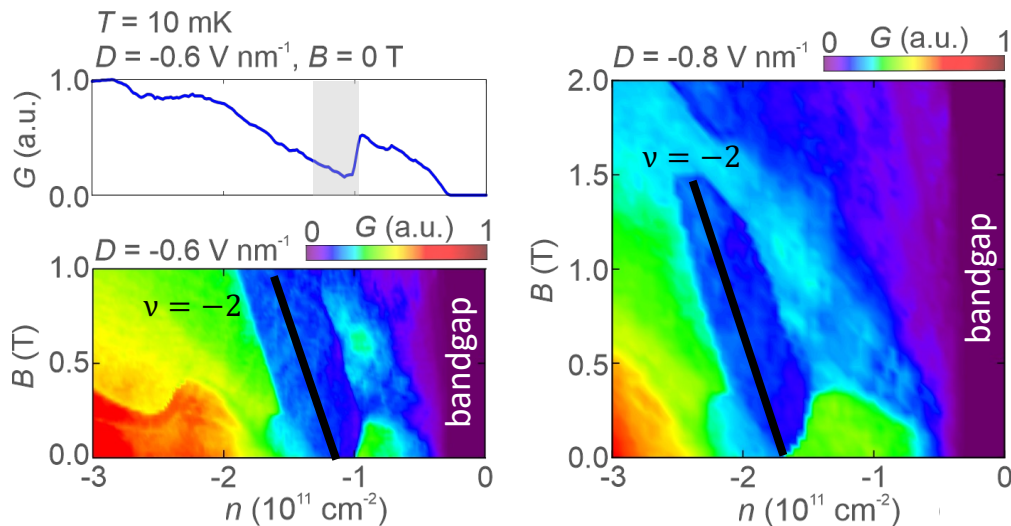
Applying an out-of-plane magnetic field



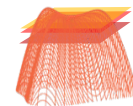
- Slope in the magnetic field ($\nu = -2$)



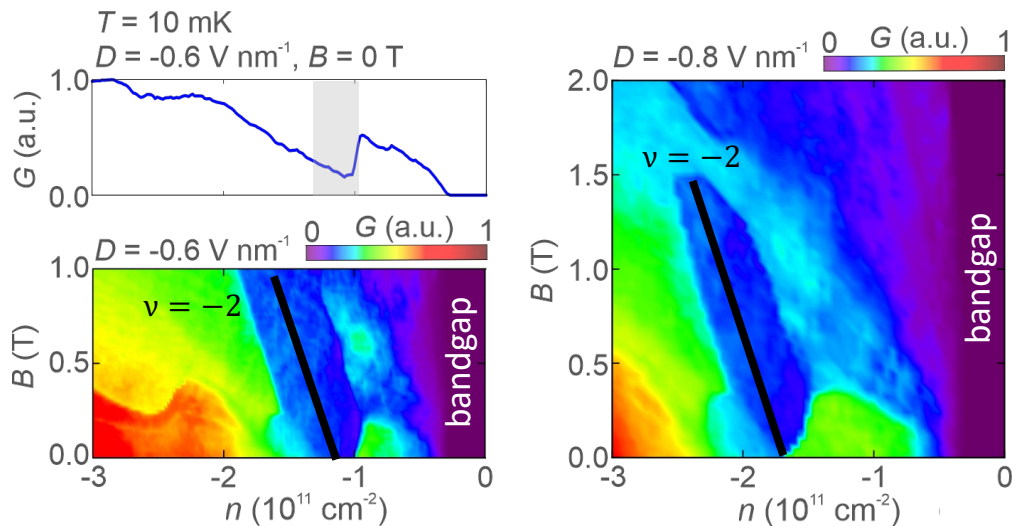
Applying an out-of-plane magnetic field



- Slope in the magnetic field ($\nu = -2$)
- Starts at finite density
- No moiré pattern



Applying an out-of-plane magnetic field



- Slope in the magnetic field ($\nu = -2$)
- Starts at finite density
- No moiré pattern



Consistent with a
Wigner Hall crystal

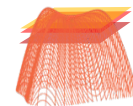
See also:

Z. Tešanović, Françoise Axel, and B. I. Halperin, *Phys. Rev. B* **39**, 8525 (1989)

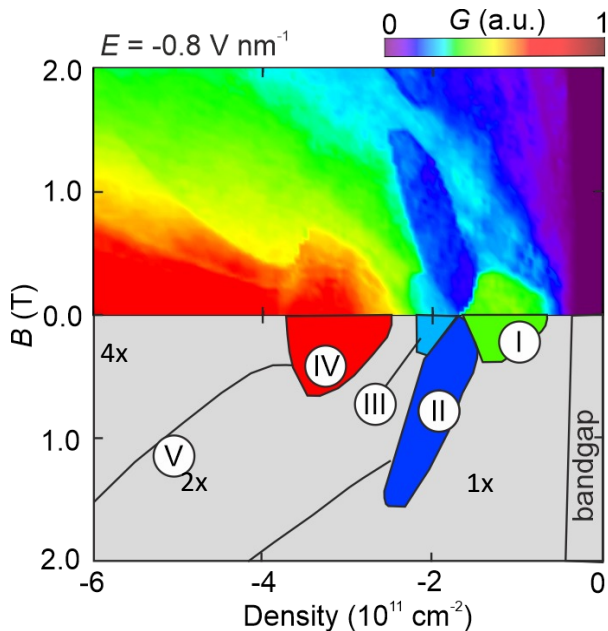
J. Dong et al., arXiv:2311.05568 (2023)

B. Zhou et al., arXiv:2311.04217 (2023)

Z. Lu et al., *Nature* **626**, 759–764 (2024)



Cascade of correlated phases

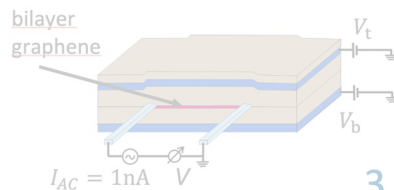


More correlated phases including:

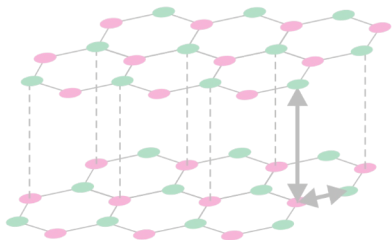
- Correlated metals
- Topologically-trivial correlated insulator

Outline

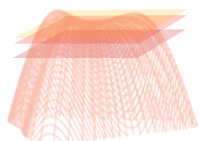
2. Transport measurements



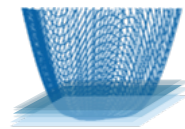
1. Bernal bilayer graphene

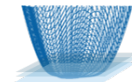


3. Correlated phases at hole-doping

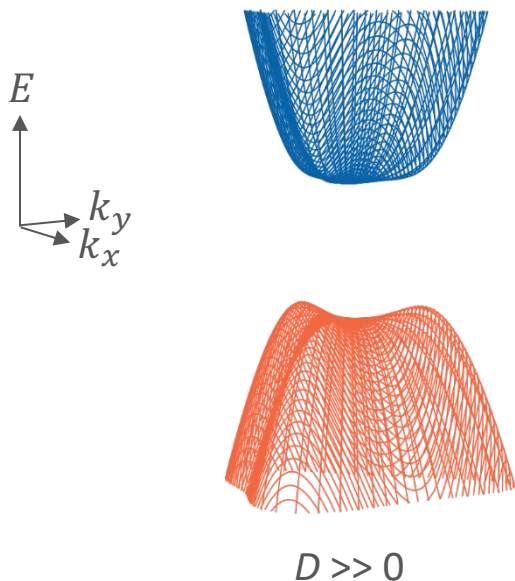


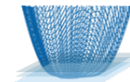
4. Correlated phases at electron-doping



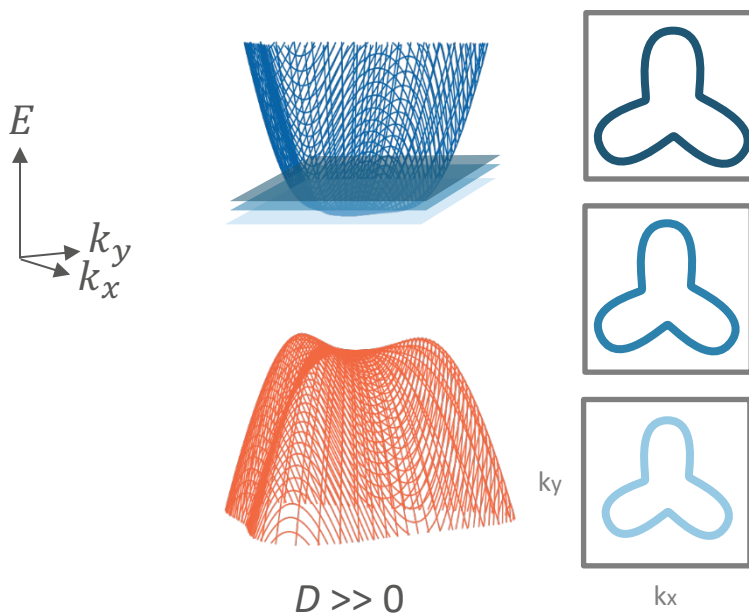


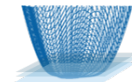
Trigonal warping in the conduction band



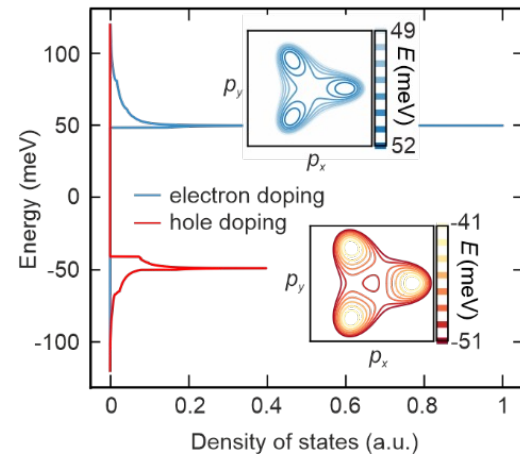
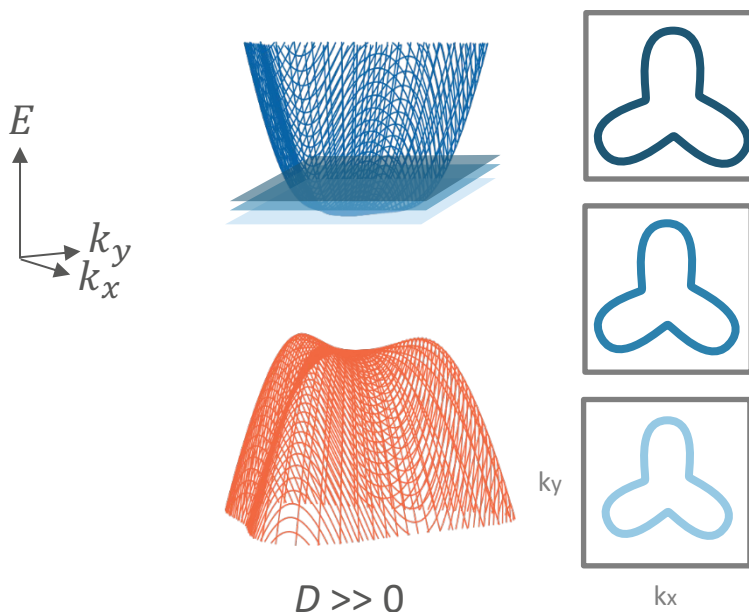


Trigonal warping in the conduction band

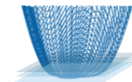




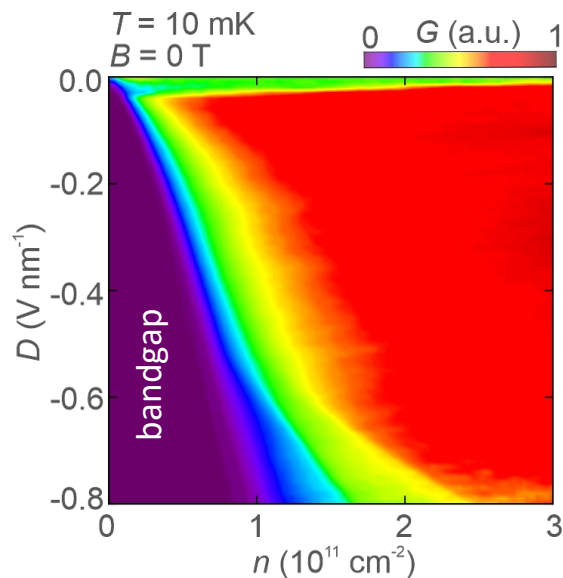
Trigonal warping in the conduction band

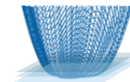


- Flat bands
- Van Hove singularity at the band edge
- High DOS

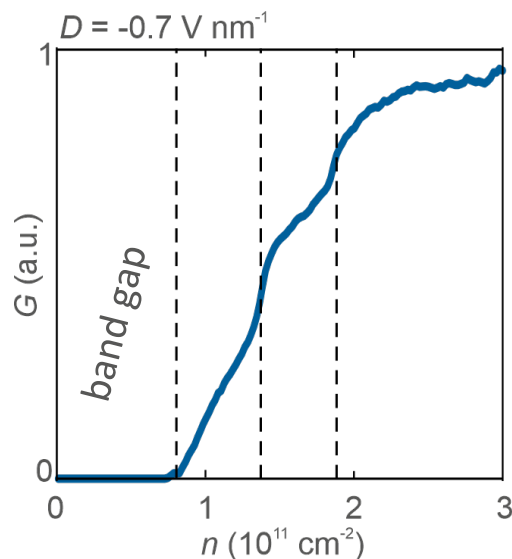
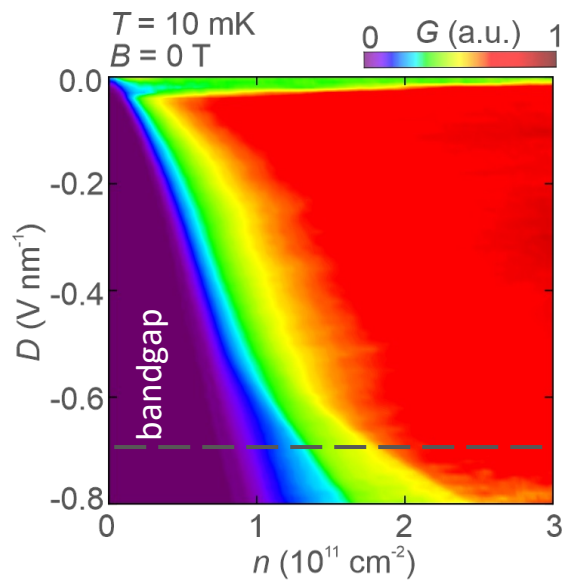


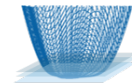
Correlated phases in electron-doped bilayer graphene



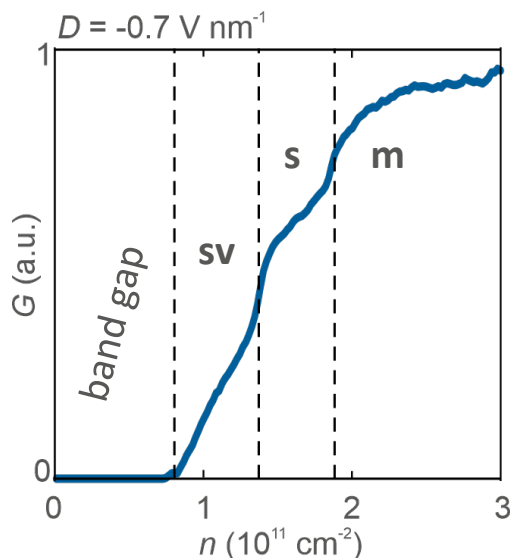
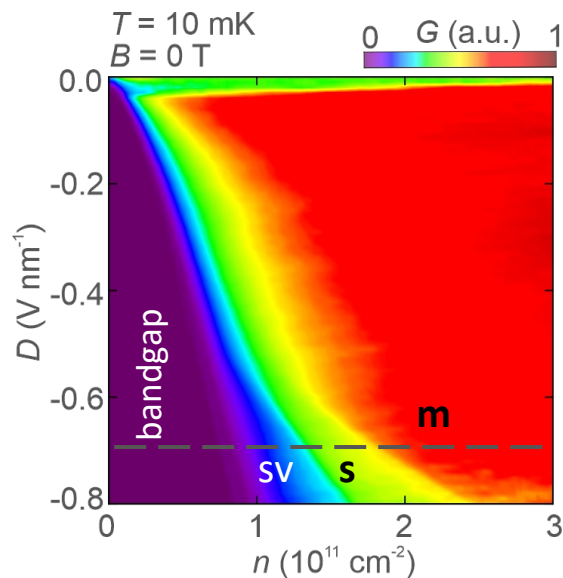


Correlated phases in electron-doped bilayer graphene





Correlated phases in electron-doped bilayer graphene

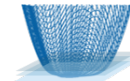


sv: spin and valley polarized

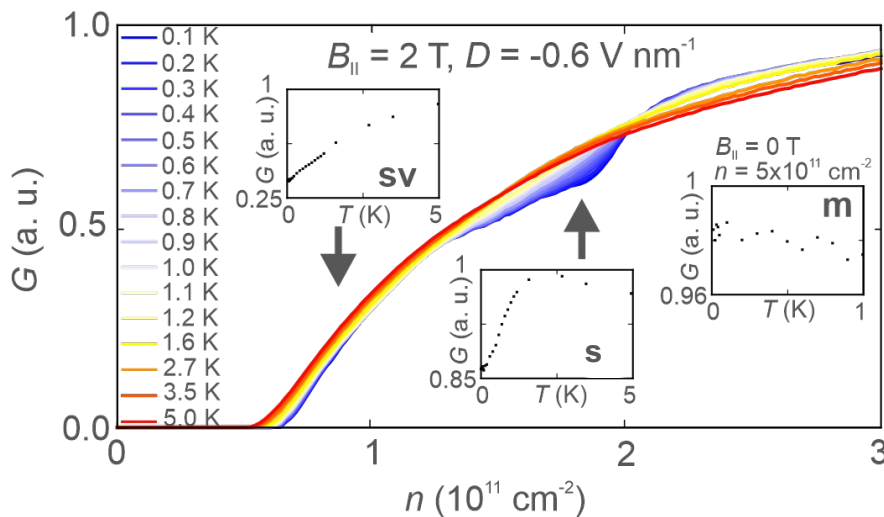
s: spin polarized

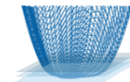
m: four-fold degenerate (not polarized)

Consistent with S. C. de la Barrera et al.,
Nature Physics **18**, 771-775 (2022)

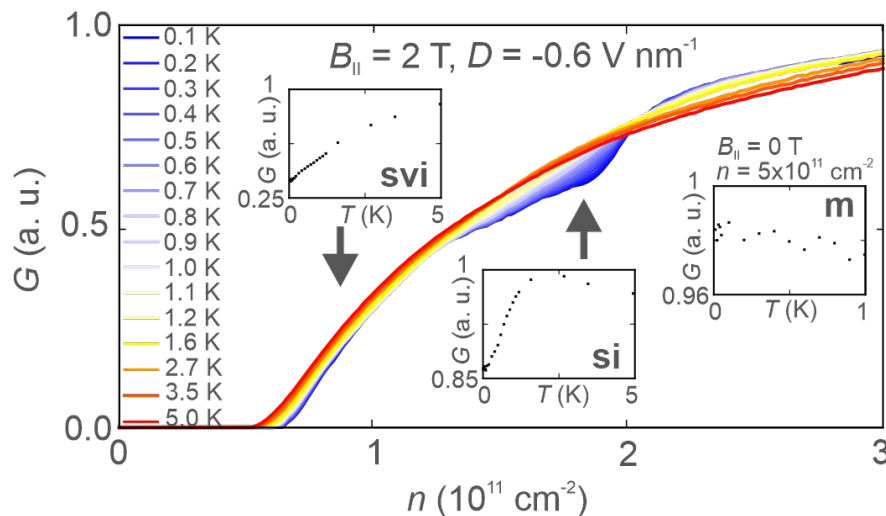


Insulating temperature dependence





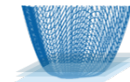
Insulating temperature dependence



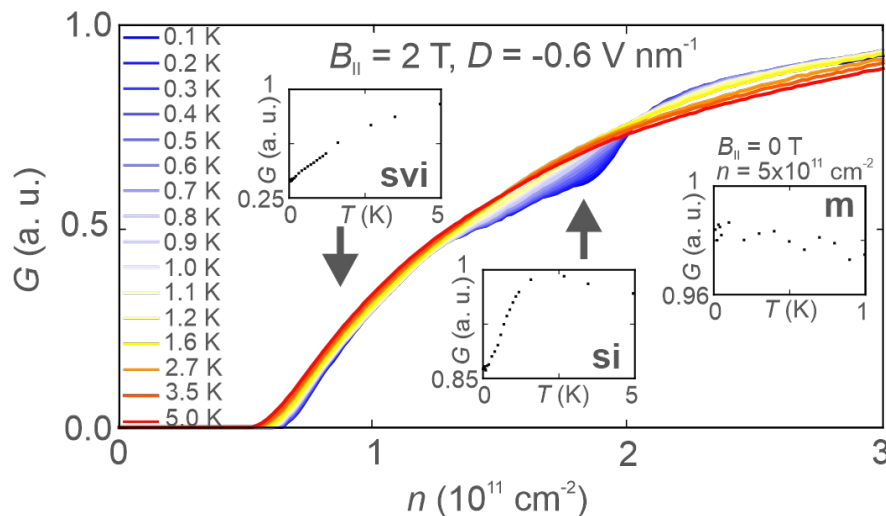
svi: spin and valley polarized (quasi-) insulator

si: spin polarized (quasi-) insulator

m: metal



Insulating temperature dependence



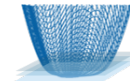
svi: spin and valley polarized (quasi-) insulator

si: spin polarized (quasi-) insulator

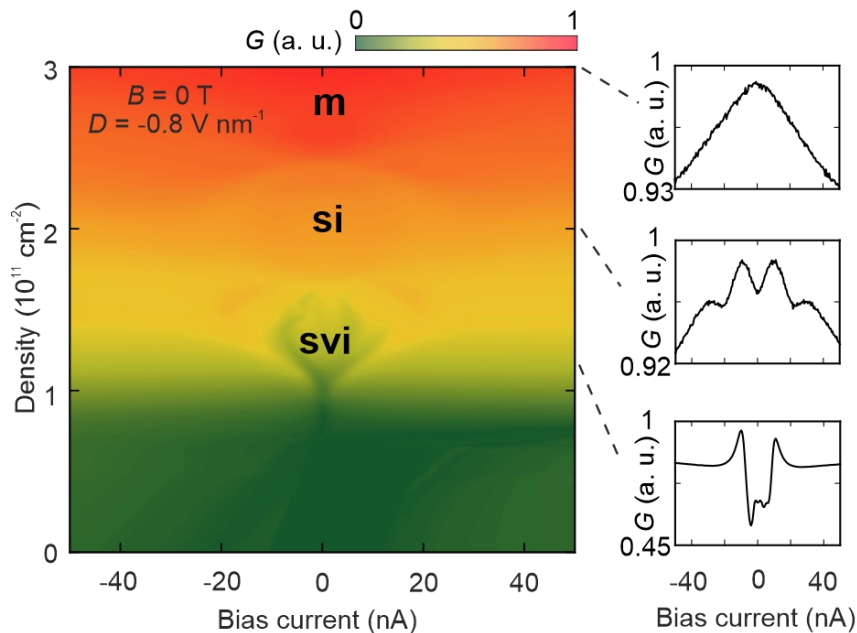
m: metal

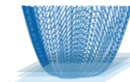


Consistent with a charge density wave or Wigner crystal

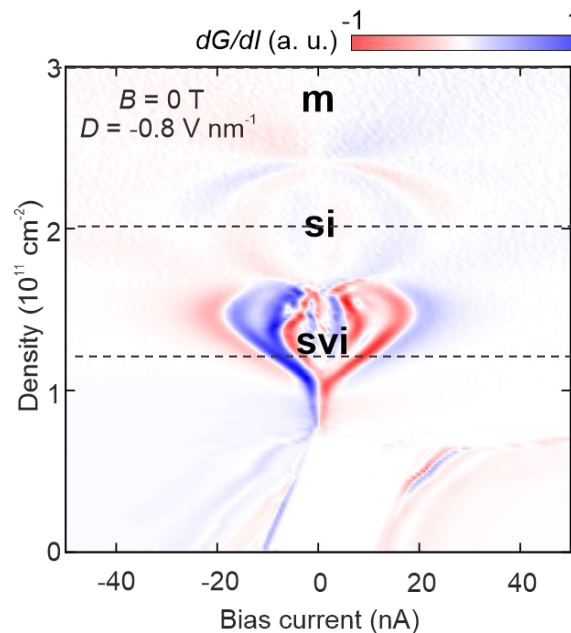
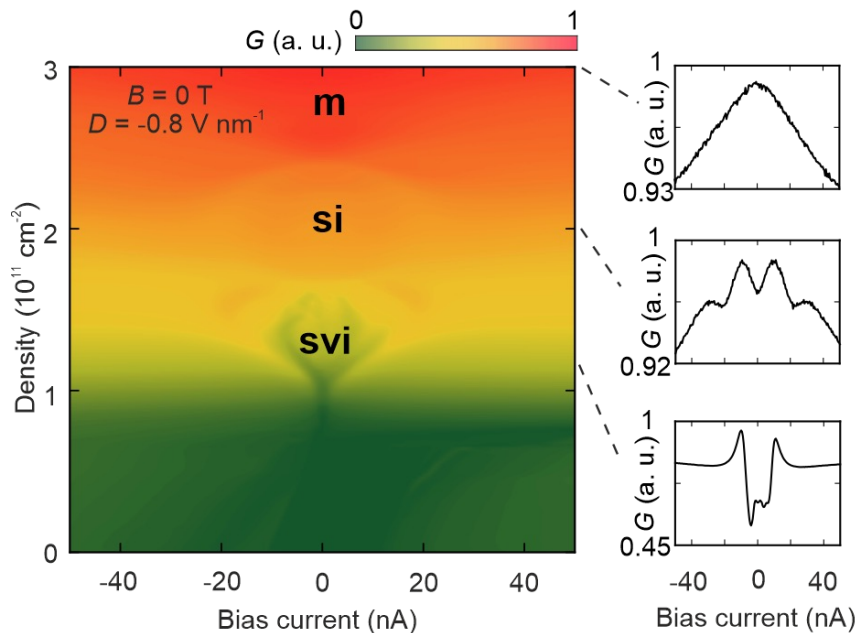


Non-linear bias current





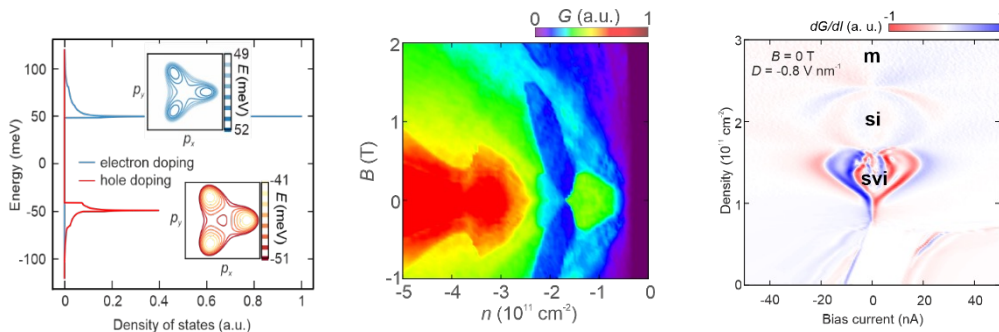
Non-linear bias current



Summary

Cascade of correlated phases in hole- and electron-doped bilayer graphene

- One correlated insulating state is consistent with a Wigner Hall crystal state
- Strong electron-hole asymmetry



Nat. Commun. **15**, 3133 (2024)
Nature **608**, 298-302 (2022)
 arXiv:2308.00827 (2023)

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